

# Aggregate Implications of Microeconomic Consumption Behavior

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## Broad Overview

Two approaches to microfoundations of consumption:

- Saltwater
  - Start with micro theory and data, aggregate
  - Conclusion: Risk, heterogeneity change everything
  - Criticism: No real GE analysis
- Freshwater
  - Start with Rep Agent (RA) model, introduce risk
  - Conclusion: Risk, heterogeneity don't matter
  - Criticism: Totally unrealistic micro implications

# Tidewater!

- GE Framework With 'Serious' Heterogeneity
- Salt and Fresh Water Frameworks are Special Cases
- Combines Advantages of Both Classes
  - Wealth Distribution 'Matters'
  - Get 'Excess Sensitivity' of  $C$
  - High MPC for  $c$
  - Fully articulated GE

# Talk Outline

- Saltwater: Microeconomic Consumption Behavior
  - Reference: Carroll (2004), Carroll (2001a)
- Freshwater: The Ramsey/Cass-Koopmans Model
  - Grad School!
- Tidewater
  - Reference: Krusell and Smith (1998), Carroll (2000a)
- Reseverations

# Micro History of Thought

- Permanent Income Hypothesis of Friedman (1957)
  - $C = E[Y] + (Y - E[Y])\kappa$  for  $\kappa \approx 0.3$
- Perfect Foresight Infinite Horizon PIH (Bewley (1977))
  - $C = (H + N)\kappa$  for  $\kappa \approx 0.03$
- Buffer Stock Models (Deaton (1991), Carroll (1992))
  - As  $M \downarrow 0$ ,  $\kappa \uparrow 1$
  - As  $M \uparrow \infty$ ,  $\kappa \downarrow r$
- Evidence
  - For median household,  $\kappa \approx 0.15 - 0.50$
  - For richer households,  $\kappa$  much smaller

# Perfect Foresight Benchmark

$$\max \sum_{t=0}^{\infty} \beta^t u(C_t)$$

$$u(C) = C^{1-\rho}/(1-\rho)$$

Initial conditions:  $M_0$  and  $P_0$

$$A_t = M_t - C_t$$

$$B_{t+1} = A_t R$$

$$M_{t+1} = B_{t+1} + P_{t+1}$$

$$P_{t+1} = GP_t$$

## Perfect Foresight Solution

$$H_t = P_t \left( \frac{1}{1 - (G/R)} \right)$$

$$\begin{aligned} \kappa &= (1 - (R\beta)^{1/\rho}/R) \\ C(M_t, P_t) &= (H_t + \underbrace{M_t - P_t}_{=B_t})\kappa \end{aligned}$$

Benchmark parameter values

$$\begin{aligned} \rho &= 2 \\ R &= 1.03 \\ \beta &= 0.97 \end{aligned}$$

imply  $\kappa \approx 0.03$ .

## Idiosyncratic Uncertainty

$$\begin{aligned} M_{t+1} &= B_{t+1} + P_{t+1}\xi_{t+1} \\ P_{t+1} &= GP_t\Psi_{t+1} \end{aligned}$$

Also assume:

- iid  $\xi$  and  $\Psi$  satisfy  $E_t[\Psi_{t+n}] = E_t[\xi_{t+n}] = 1 \forall n > 0$
- With small probability  $p$ ,  $\xi = 0$  (unemployment)
- Impatience:  $R\beta E[(G\Psi)^{-\rho}] < 1$

# Normalized Solution

Problem has a solution of the form

$$C(M, P) = P \underbrace{c(M/P)}_{=m}$$

If we 'turn off' the uncertainty (assume  $\Psi_t = \xi_t = 1 \forall t$ ), the solution is

$$c(m) = (h_t + \underbrace{m_t - 1}_{b_t}) \kappa$$

# Effect of Uncertainty

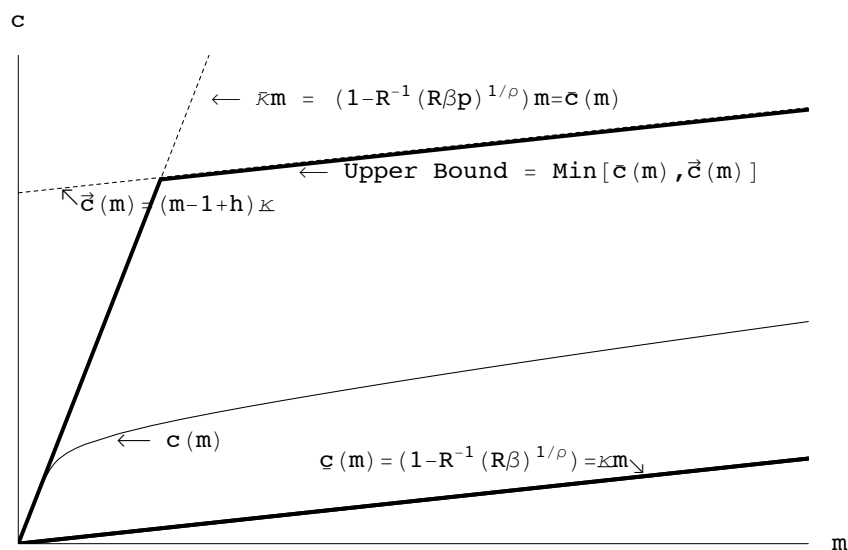


Figure: Concave  $c(m)$  and Its Bounds

# Marginal Propensity to Consume

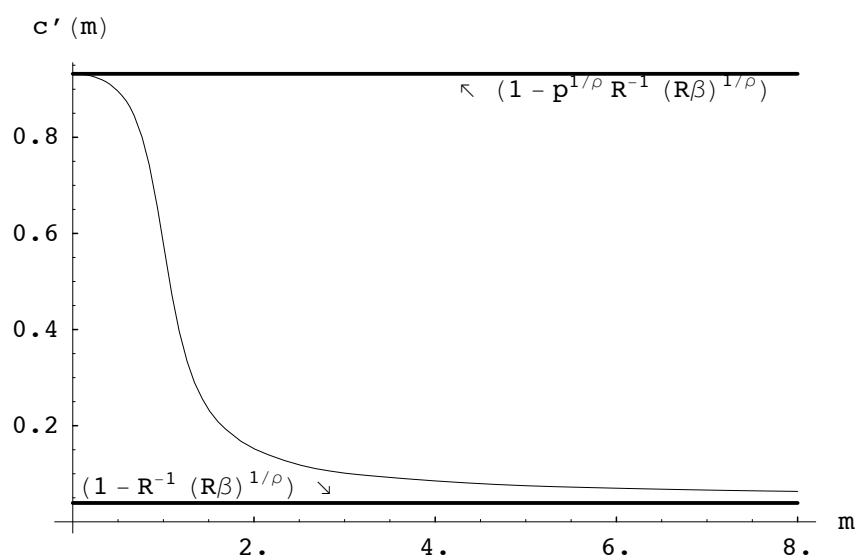


Figure: The MPC and Its Bounds

## Key Intuition

- Impatience: At  $m_t = \infty$ ,  $C > P$  so  $E_t[m_{t+1}] < m_t$
- Precaution: At  $m_t = 0$ ,  $C = 0 < P$  so  $E_t[m_{t+1}] > m_t$

These imply:

- A 'target' level of wealth exists at which impatience exactly matches prudence, and  $C = P$
- Actual wealth will be distributed around the target

# Matching the Median Household

Income Growth Factor	Mean $a$	Median $a$	Aggregate Consumption Growth	Mean MPC	Frac With $a < 0$	Frac With $a = 0$
Panel A. Baseline Model, No Constraints						
G=1.03	0.43	0.40	1.030	0.330	0.000	0.000
G=1.00	2.26	2.06	1.000	0.064	0.000	0.000
Panel B. Strict Liquidity Constraints						
G=1.03	0.28	0.24	1.030	0.361	0.000	0.070
G=1.00	2.28	2.06	1.000	0.065	0.000	0.000
Panel C. Borrowing Up To 0.3 Allowed						
G=1.03	-0.03	-0.06	1.030	0.361	0.611	0.000
G=1.00	1.94	1.71	1.000	0.064	0.023	0.000

Source: Carroll (2001b)

# Constraints Don't Matter ...

- Under uncertainty, prudence acts like a self-imposed liquidity constraint
- Eqbm behavior of consumers in a constrained model almost indistinguishable from eqbm behavior of consumers in the corresponding unconstrained model. (Carroll (2001b))

## ...Except When They Change

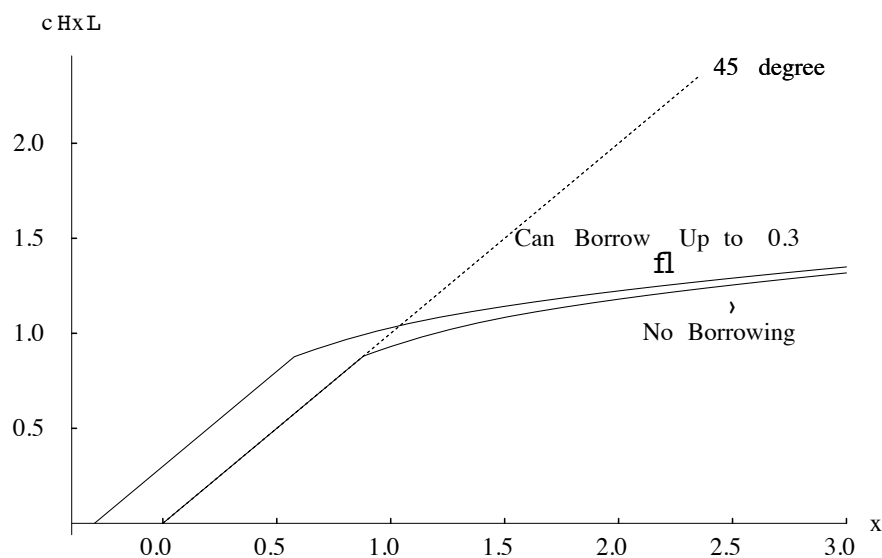


Figure: Strict and Looser Liquidity Constraints

## Summing Up

- Theory says  $c(m)$  is concave
  - High MPC for people with low wealth
  - Low MPC for people with high wealth
- Target assets  $a^*$  depend on patience
  - Small differences in  $G$  produce large  $a$  differences
- Distribution could matter a lot in SR
  - Tax changes targeting poor will have much bigger kick
- Constraints have modest long-run consequences
- Changes in constraints can have a big SR effect



# The Stochastic Growth Model

- Turn off the transitory shocks:  $\xi = 1$
- Aggregate production function:  $F(K, P) = K^\gamma P^{1-\gamma}$
- Introduce depreciation:  $K_{t+1} = A_t \bar{\Gamma}$

Normalize again, obtaining

$$\begin{aligned} k_{t+1} &= (\bar{\Gamma}/G\Psi_{t+1})a_t \\ m_{t+1} &= k_{t+1} + k_{t+1}^\gamma \end{aligned}$$

# Calibrating Stochastic Growth Model

$$\begin{aligned} \alpha &= 0.36 \\ \bar{\Gamma} &= 1.10 \\ G &= 1.00 \\ \beta &= 0.96 \end{aligned}$$

Bottom Line:

- Typically calibrated to match  $K/Y \approx 3 \sim 4$
- RA is very rich!

## In a Nutshell

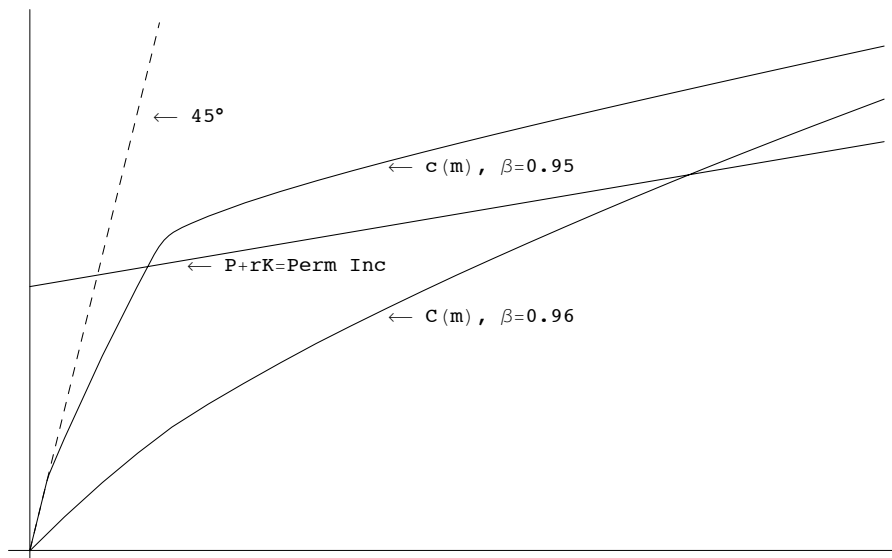


Figure: Salt and Freshwater Models

## A Tidewater Model

- Take saltwater model and allow  $F(K, L)$
- Take freshwater model and allow  $\xi_{i,t}$   
Aiyagari (1994), Krusell and Smith (1998)
- Conclusion: Looks just like freshwater model
  - Eqbm  $K$  rises maybe 1 percent
  - MPC remains small, close to value in RCK model
  - Dynamics, impulse responses indistinguishable

## Why?

Instead of 1 rep agent at SS  $K/Y$  ratio of 3.5

- Group of agents distributed around a  $K/Y$  of 3.0-4.0
- But behavior of these consumers is very similar to the RA consumer
- Looks nothing like micro data
  - Bottom 50 percent of HH's own 5 percent of wealth
  - Lots of evidence of high MPC's among them

## Solution: 'Serious' Heterogeneity

- Uninsurable shocks aren't enough
- Need some people with low 'target' wealth
- Alternatives:
  - Patient vs impatient
  - Young vs old
  - Fast-growing vs slow-growing occupations
  - Low vs high rates of return on saving
- Long run  $K^*$  will depend on 'patient'
- Short run  $C$  will depend on wealth distribution

## An Example: Krusell and Smith (1998)

- Proportion  $\lambda = 0.66$  are impatient,  $\beta = 0.90$
- Proportion  $(1 - \lambda) = 0.34$  are patient,  $\beta = 0.96$

Model	$K/W$	$K/W$ By Percentile		Agg MPC
		Bottom 66	Top 34	
Fresh	3.929	-	-	0.043
Tide	3.963	3.48	4.95	0.045
Tide+Hetero	3.910	0.39	11.06	0.187

Source: Carroll (2000a)

## Implications

- Fiscal policy
  - $c'$  much higher for low income HH's
  - Stabilizing  $C$  depends on stabilizing  $m$  at bottom
- Monetary policy
  - Mainly works through effects on the 'patient'
    - The impatient finance most  $c$  through  $y$
  - Caveat: This ignores durables

## Implications (cont.)

- Uncertainty Matters
  - Plausible Movement in Uncertainty Can Move  $C$
  - Worth trying to measure:
    - Consumer sentiment
    - Composition of spending
    - Read the newspaper!

## Reservations: Excess Smoothness

- $C$  is Still Too Predictable
  - Ludvigson and Michaelides (2001)
- Explanations:
  - Habit formation (Fuhrer (2000))
  - 'Sticky expectations' (Carroll (2003))

## Sticky Expectations

- $\text{var}(\Delta \log \psi) \approx 100\text{var}(\Delta \log \Psi)$

Suppose people only notice macro news with some probability  $\gamma$   
Then

$$\Delta \log C_{t+1} \approx (1 - \gamma)\Delta \log C_t + \epsilon_{t+1}$$

which can explain excess smoothness

## Reservations: Saving and Growth

- All these models imply  $G \uparrow \Rightarrow S \downarrow$ 
  - If you're going to be rich, why save now?
- Data say  $G \uparrow \Rightarrow S \uparrow$ 
  - Japan, Korea, HPAE's
  - OECD after party slowdown
- Habits? (Carroll, Overland, and Weil (2000))

## Reservations: Bill Gates

- About 1/4 of K owned by richest 1 pct
- No standard model can match this
- Two modifications seem necessary:
  - Entrepreneurship (e.g. Quadrini (1999))
    - Bill Gates isn't rich because he's patient
  - 'Capitalist spirit' utility
    - It's fun to be rich (Carroll (2000b))

## Conclusions

- Micro
  - Tidewater model with serious heterogeneity
  - Behavior depends on wealth
- Macro Short Run
  - Excess Smoothness: Tidewater Goes Partway
  - Need Something Else
    - 'Sticky Expectations'
    - Habits
- Macro Medium Run
  - Saving and Growth
  - Capitalist Spirit

- Aiyagari, S. R. (1994). Uninsured idiosyncratic risk and aggregate saving. *Quarterly Journal of Economics*, 109, 659–684.
- Bewley, T. (1977). The permanent income hypothesis: A theoretical formulation. *Journal of Economic Theory*, 16, 252–292.
- Carroll, C. D. (1992). The buffer-stock theory of saving: Some macroeconomic evidence. *Brookings Papers on Economic Activity*, 1992(2), 61-156. (Available at <http://econ.jhu.edu/people/ccarroll/BufferStockBPEA.pdf>)
- Carroll, C. D. (2000a, May). Requiem for the representative consumer? aggregate implications of microeconomic consumption behavior. *American Economic Review, Papers and Proceedings*, 90(2), 110–115. (Available at <http://econ.jhu.edu/people/ccarroll/RequiemFull.pdf>)
- Carroll, C. D. (2000b). Why Do the Rich Save So Much? In J. B. Slemrod (Ed.), *Does Atlas Shrug? The Economic Consequences of Taxing the Rich*. Harvard University Press. (Available at <http://econ.jhu.edu/people/ccarroll/Why.pdf>)

- Carroll, C. D. (2001a, Summer). A theory of the consumption function, with and without liquidity constraints. *Journal of Economic Perspectives*, 15(3), 23-46. (  
<http://econ.jhu.edu/people/ccarroll/ATheoryv3JEP.pdf> (as published)  
<http://econ.jhu.edu/people/ccarroll/ATheoryv3NBER.pdf> (more rigorous),  
<http://econ.jhu.edu/people/ccarroll/ATheoryMath.zip> (software archive))
- Carroll, C. D. (2001b). A theory of the consumption function, with and without liquidity constraints (expanded version). *NBER Working Paper Number W8387*. (  
JEP Version:  
<http://econ.jhu.edu/people/ccarroll/ATheoryv3JEP.pdf>  
NBER Working Paper:  
<http://econ.jhu.edu/people/ccarroll/ATheoryv3NBER.pdf>  
Programs to generate all theoretical results:



<http://econ.jhu.edu/people/ccarroll/ATheoryMath.zip>)

- Carroll, C. D. (2003). Macroeconomic Expectations of Households and Professional Forecasters. *Quarterly Journal of Economics*, 118(1), 269–298. (Available at <http://econ.jhu.edu/people/ccarroll/epidemiologyQJE.pdf>)
- Carroll, C. D. (2004, November). Theoretical Foundations of Buffer Stock Saving. *NBER Working Paper No. 10867 (Status: Revise and Resubmit, Review of Economic Studies)*. (Latest version available at <http://econ.jhu.edu/people/ccarroll/BufferStockTheory.pdf>)
- Carroll, C. D., Overland, J. R., & Weil, D. N. (2000, June). Saving and Growth with Habit Formation. *American Economic Review*, 90(3), 341–355. Available from <http://econ.jhu.edu/people/ccarroll/AERHabits.pdf> (Available at <http://econ.jhu.edu/people/ccarroll/AERHabits.pdf>)
- Deaton, A. S. (1991). Saving and liquidity constraints. *Econometrica*, 59,

1221-1248. (Available at <http://ideas.repec.org/a/ecm/emetrp/v59y1991i5p1221-48.html>)

- Friedman, M. A. (1957). *A theory of the consumption function*. Princeton University Press.
- Fuhrer, J. C. (2000, June). An optimizing model for monetary policy: Can habit formation help? *American Economic Review*, 90(3).
- Krusell, P., & Smith, A. A. (1998). Income and wealth heterogeneity in the macroeconomy. *Journal of Political Economy*, 106(5), 867–896.
- Ludvigson, S., & Michaelides, A. (2001, June). Does buffer stock saving explain the smoothness and excess sensitivity of consumption? *American Economic Review*, 91(3), 631–647.
- Quadrini, V. (1999). The importance of entrepreneurship for wealth concentration and mobility. *The Review of Income and Wealth*, 45, 1–20.