The Distribution of Wealth and the Marginal Propensity to Consume

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Why Worry About the MPC ($\equiv \kappa$)?

- Big 'stimulus' tax cuts
- Keynesian multipliers should be big in liquidity trap
- Crude Keynesianism: Transitory tax cut multiplier is $1/(1-\kappa)-1$
 - \sim If $\kappa = 0.75$ then multiplier is 4-1=3
 - If $\kappa=0.05$ then multiplier is only pprox 0.05

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Nobody trying to make a forecast in 2008-2010 would ask:

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Our Claim: Heterogeneity Is Key To Modeling the MPC

Clarida (2012): Missing this is why DSGE models failed

- Theory: HH c function is *concave* in market resources *m*
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 - response to financial shocks (say, revised view of $\sigma_{\rm starts}^2$)

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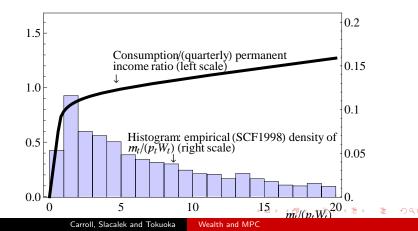
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Consumption Concavity and Wealth Heterogeneity



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Microeconomics of Consumption

- c chosen optimally: Want to smooth c in light of y fluctuations
- Single most important thing to get right is income dynamics!
- With smooth c, income dynamics drive everything!
 - Saving/dissaving: Depends on whether $\mathbb{E}[\Delta y] \uparrow$ or $\mathbb{E}[\Delta y] \downarrow$
 - Wealth distribution depends on integration of saving
- Cardinal sin: Assume crazy income dynamics
 - No end can justify this means
 - Throws out the defining core of the intellectual framework

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Our Goal: "Serious" Microfoundations

- Sensible microeconomic income process
- Finite lifetimes
- Match wealth distribution
 - Here, achieved by preference heterogeneity.
 - View it as a proxy for many kinds of heterogeneity.

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Requires three changes to well-known Krusell-Smith model:

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- 2 Match empirical wealth distribution
- Back out optimal C and MPC out of transitory income
- Is MPC in line with empirical estimates?

Our Question:

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Friedman (1957): Permanent Income Hypothesis

 $\begin{array}{rcl} Y_t &=& P_t + T_t \\ C_t &=& P_t \end{array}$

Progress since then

- Micro data: Friedman description of income shocks works well
- Math: Friedman's words well describe optimal solution to dynamic stochastic optimization problem of impatient consumers with geometric discounting under CRRA utility with uninsurable idiosyncratic risk calibrated using these micro income dynamics (!)

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Income process Decision Problem What Happens After Death? There Is an Ergodic Distribution of Permanent Income Parameter Values Annual Income Variances Our Strategy

Our (Micro) Income Process

Idiosyncratic (household) income process is logarithmic Friedman:

 p_t = permanent income ξ_t = transitory income ψ_{t+1} = permanent shock W = aggregate wage rate

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Further Details of Income Process

Modifications from Carroll (1992):

Trans income ξ_t incorporates unemployment insurance:

$$\xi_t = \mu$$
 with probability u
= $(1 - \tau)\overline{\ell}\theta_t$ with probability $1 - u$

 μ is UI when unemployed

 τ is the rate of tax collected for the unemployment benefits

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Model Without Aggr Uncertainty: Decision Problem

$$v(m_t) = \max_{\{c_t\}} u(c_t) + \beta \not D \mathbb{E}_t \left[\psi_{t+1}^{1-\rho} v(m_{t+1}) \right]$$
s.t.
$$a_t = m_t - c_t$$

$$a_t \ge 0$$

$$k_{t+1} = a_t / (\not D \psi_{t+1})$$

$$m_{t+1} = (\neg + r) k_{t+1} + \xi_{t+1}$$

$$r = \alpha a(\not K / \bar{\ell} \bm{L})^{\alpha - 1}$$

Variables normalized by $p_t W$

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What Happens After Death?

- You are replaced by a new agent whose permanent income is equal to the population mean
- Prevents the population distribution of permanent income from spreading out

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Ergodic Distribution of Permanent Income

Exists, if death eliminates permanent shocks:

 $\mathcal{D}\mathbb{E}[\psi^2] < 1.$

Holds.

Population mean of p^2 :

$$\mathbb{M}[p^2] = \left(\frac{\mathsf{D}}{1 - \mathcal{D}\mathbb{E}[\psi^2]}\right)$$

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Parameter Values

• β , ρ , α , δ , $\bar{\ell}$, μ , and u taken from JEDC special volume

• Key new parameter values:

Description	Param	Value	Source
Prob of Death per Quarter Variance of Log ψ_t Variance of Log θ_t	$\begin{array}{c} D \\ \sigma_{\psi}^2 \\ \sigma_{\theta}^2 \end{array}$	$0.005 \\ 0.016/4 \\ 0.010 imes 4$	Life span of 50 years Carroll (1992); SCF Carroll (1992)

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Image: A mathematical states of the state

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Annual Income, Earnings, or Wage Variances

Our parameters	$\sigma_\psi^2 \ 0.016$	σ_{ξ}^2 0.010
Carroll (1992) Storesletten, Telmer, and Yaron (2004) Meghir and Pistaferri (2004)* Low, Meghir, and Pistaferri (2010)	0.016 0.008–0.026 0.031 0.011 0.010–0.030	0.010 0.316 0.032 0.029-0.055
Blundell, Pistaferri, and Preston (2008a)* Implied by KS-JEDC Implied by Castaneda et al. (2003)	0.000 0.028	0.029-0.055 0.038 0.004

* Meghir and Pistaferri (2004) and Blundell, Pistaferri, and Preston (2008a) assume that the transitory component is serially correlated (an MA process), and report the variance of a subelement of the transitory component. σ_{ξ}^2 for these articles are calculated using their MA estimates.

Income process Decision Problem What Happens After Death? There Is an Ergodic Distribution of Permanent Income Parameter Values Annual Income Variances Our Strategy

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Typology of Our Models

Three Dimensions



Income process Decision Problem What Happens After Death? There Is an Ergodic Distribution of Permanent Income Parameter Values Annual Income Variances Our Strategy

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Typology of Our Models

Three Dimensions

$\bullet \quad \text{Discount Factor } \beta$

- ' β -Point' model: Single discount factor
- 'β-Dist' model: Uniformly distributed discount factor

- (No)
- Krusell–Smith
- Friedman/Buffer Stock
- Impirical Wealth Variable to Match
 - Net Worth
 - Liquid Financial Assets

Income process Decision Problem What Happens After Death? There Is an Ergodic Distribution of Permanent Income Parameter Values Annual Income Variances Our Strategy

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Income process Decision Problem What Happens After Death? There Is an Ergodic Distribution of Permanent Income Parameter Values Annual Income Variances Our Strategy

Dimension 1: Estimation of β -Point and β -Dist

' β -Point' model

• 'Estimate' single \dot{eta} by matching the capital–output ratio

β-Dist' model—Heterogenous Impatience

- Assume uniformly distributed β across households
- Estimate the band [β − ∇, β + ∇] by minimizing distance between model (w) and data (ω) net worth held by the top 20, 40, 60, 80%

$$\min_{\{\hat{\beta}, \nabla\}} \sum_{i=20, 40, 60, 80} (w_i - \omega_i)^2,$$

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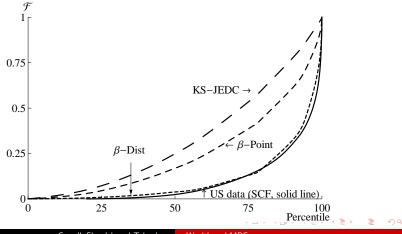
Results: Wealth Distribution

Micro Income Process								
	Friedman/Buffer Stock		KS-JEDC	KS-	KS-Orig [◊]			
	Point Discount Factor [‡]	Uniformly Distributed Discount	Our solution		Hetero		Hetero	
	β -Point	Factors* β -Dist				U.S. Data*		
Top 1%	10.	26.4	3.	3.0	24.0	29.6		
Top 20%	55.1	83.1	39.7	35.0	88.0	79.5		
Top 40%	76.9	93.7	65.4			92.9		
Top 60%	90.1	97.4	83.5			98.7		
Top 80%	97.5	99.3	95.1			100.4		
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Carroll, Slacalek and Tokuoka Wealth and MPC

Income process Decision Problem What Happens After Death? There Is an Ergodic Distribution of Permanent Income Parameter Values Annual Income Variances Our Strategy

Results: Wealth Distribution



Carroll, Slacalek and Tokuoka Wealth and MPC

Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

Dimension 2.a: Adding KS Aggregate Shocks

Model with KS Aggregate Shocks: Assumptions

- Only two aggregate states (good or bad)
- Aggregate productivity $a_t = 1 \pm \triangle^a$
- Unemployment rate u depends on the state (u^g or u^b)

Parameter values for aggregate shocks from Krusell and Smith (1998)

Parameter	Value
\triangle^a	0.01
u ^g	0.04
и ^ь	0.10
Agg transition probability	0.125

Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

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Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

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- HH needs to forecast $\boldsymbol{k}_t \equiv \boldsymbol{K}_t / \bar{\ell}_t \boldsymbol{L}_t$ since it determines future interest rates and wages.
- Two broad approaches
 - Direct computation of the system's law of motion Advantage: fast, accurate
 - Simulations (iterate until convergence) Advantage: directly generate micro data ⇒ we do

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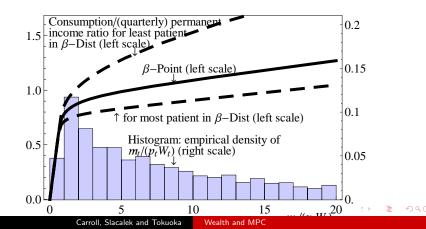
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Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

Marginal Propensity to Consume & Net Worth



Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

Results: MPC (in Annual Terms)

	Micro Income Process			
	Friedman/	Friedman/Buffer Stock		
	β -Point	β -Dist	Our solution	
Overall average	0.1	0.23	0.05	
By wealth/permanent income ratio				
Top 1%	0.06	0.05	0.04	
Тор 20%	0.06	0.06	0.04	
Тор 40%	0.06	0.08	0.04	
Тор 60%	0.07	0.12	0.04	
Bottom 1/2	0.13	0.35	0.05	
By employment status				
Employed	0.09	0.2	0.05	
Unemployed	0.23	<u>,0.53 ,</u>	< ≥ > 0.06, ≥	

Carroll, Slacalek and Tokuoka Wealth and MPC

Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

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Estimates of MPC in the Data: $\sim 0.2-0.6$

	Cons	sumption Meas	sure		
Authors	Nondurables	Durables	Total PCE	Horizon*	Event/Sa
Blundell, Pistaferri, and Preston (2008b) [‡]	0.05				Estimatio
Coronado, Lupton, and Sheiner (2005)			0.36	1 Year	2003 Ta×
Hausman (2012)			0.6-0.75	1 Year	1936 Vet
Jappelli and Pistaferri (2013)	0.48				Italy, 201
Johnson, Parker, and Souleles (2009)	~ 0.25			3 Months	2003 Chi
Lusardi (1996) [‡]	0.2-0.5				Estimatio
Parker (1999)	0.2			3 Months	Estimatio
Parker, Souleles, Johnson, and McClelland (2011)	0.12-0.30		0.50-0.90	3 Months	2008 Eco
Sahm, Shapiro, and Slemrod (2010)			$\sim 1/3$	1 Year	2008 Eco
Shapiro and Slemrod (2009)			$\sim 1/3$	1 Year	2008 Eco
Souleles (1999)	0.045-0.09	0.29-0.54	0.34-0.64	3 Months	Estimatio
Souleles (2002)	0.6-0.9			1 Year	The Rea
					of the Ea

Notes: [‡]: elasticity.

Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

Dimension 2.b: Adding FBS Aggregate Shocks

Friedman/Buffer Stock Shocks

- Motivation:
 - More plausible and tractable aggregate process, also simpler
- Eliminates 'good' and 'bad' aggregate state
- Aggregate production function: $K_t^{\alpha}(L_t)^{1-1}$
 - P_f is aggregate permanent productivity.
 - $P_{t+1} = P_t \Psi_{t+1}$
 - $* \equiv_l$ is the aggregate transitory shock.
- Parameter values estimated from U.S. data:

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Carroll, Slacalek and Tokuoka	Wealth and MPC				

Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

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- Parameter values estimated from U.S. data:

Description	Parameter	Value			
Variance of Log Ψ_t	σ_{Ψ}^2	0.00004			
Variance of Log Ξ_t	σ_{Ξ}^2	0.00001.	◆憲→	₹	গ ৎ (
Carroll. Slacalek and Tokuoka	Wealth and MPC				

Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

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Results

Our/FBS model

- A few times faster than solving KS model
- The results are similar to those under KS aggregate shocks
- Average MPC
 - Matching net worth: 0.2
 - Matching liquid financial assets: 0.42

Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

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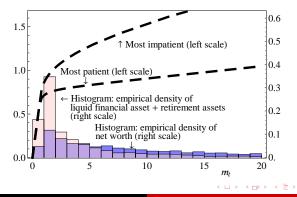
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Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

Dimension 3: Matching Net Worth vs Liquid Financial (and Retirement) Assets



Carroll, Slacalek and Tokuoka Wealth and MPC

Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

Match Net Worth vs Liquid Financial Assets

- Buffer stock saving driven by accumulation of liquidity
- May make more sense to match liquid (and retirement) assets (Hall (2011), Kaplan and Violante (2011))

	$egin{array}{c} eta \ - Dist \ \hline Net Worth & Liq Fin and Ret Asset \end{array}$		
Overall average	0.23	0.44	
By wealth/permanent income ratio			
Top 1%	0.05	0.12	
Тор 20%	0.06	0.13	
Тор 40%	0.08	0.2	
Тор 60%	0.12	0.28	
Bottom 1/2	0.35	0.59	

Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

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	$\frac{\beta - \text{Dist}}{\text{Net Worth}}$		
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Krusell–Smith Solution Method Results: Marginal Propensity to Consume Permanent/Transitory Aggregate Shocks

Match Net Worth vs Liquid Financial Assets

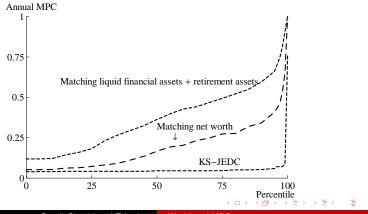
- Buffer stock saving driven by accumulation of liquidity
- May make more sense to match liquid (and retirement) assets (Hall (2011), Kaplan and Violante (2011))
- Average MPC Increases Substantially: $0.19 \uparrow 0.39$

	Net Worth	β -Dist Liq Fin and Ret Assets
Overall average	0.23	0.44
By wealth/permanent income ratio		
Top 1%	0.05	0.12
Тор 20%	0.06	0.13
Тор 40%	0.08	0.2
Тор 60%	0.12	0.28
Bottom 1/2	0.35	0.59

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Distribution of MPCs

Wealth heterogeneity translates into heterogeneity in MPCs



Carroll, Slacalek and Tokuoka Wealth and MPC

Conclusions

• Definition of "serious" microfoundations: Model that matches

- Income Dynamics
- Wealth Distribution
- The model produces more plausible implications about MPC.
- Version with more plausible aggregate specification is simpler, faster, better in every way!

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