

Formula Sheet for Econ 367 Final Exam

- $APR = n * \{ [1 + EAR]^{1/n} - 1 \}$

- Compounding. $V(0)$ today is worth $V(n) = V(0) * \exp(rn)$ in n periods. Hence $r = \frac{\ln(V(n)) - \ln(V(0))}{n}$

- Present Value: $P = \frac{C(1)}{1+r} + \frac{C(2)}{(1+r)^2} \dots + \frac{C(T)}{(1+r)^T}$

- Suppose that X_1, X_2, \dots, X_n are random variables and k_1, k_2, \dots, k_n are constants. Then

$$E(\sum k_j X_j) = \sum k_j E(X_j) \text{ and } Var(\sum k_j X_j) = \sum_{i=1}^n \sum_{j=1}^n k_i k_j Cov(X_i, X_j)$$

- Minimum Variance Portfolio weights (2 assets): $w_D = \frac{\sigma_E^2 - Cov(R_D, R_E)}{\sigma_E^2 + \sigma_D^2 - 2Cov(R_D, R_E)}$ and $w_E = 1 - w_D$

- Maximum Sharpe Ratio Portfolio weights (2 assets): $w_D = \frac{E(R_D)\sigma_E^2 - E(R_E)Cov(R_D, R_E)}{E(R_D)\sigma_E^2 + E(R_E)\sigma_D^2 - [E(R_D) + E(R_E)]Cov(R_D, R_E)}$

and $w_E = 1 - w_D$ where R_D and R_E are excess returns over the riskfree rate

- Optimal complete portfolio. If an investor has a utility function $E(r) - \frac{A}{2}\sigma^2$ then the weight in the tangent portfolio

will be $\frac{E(r_p) - r_f}{A\sigma_p^2}$ where r_p is the return on the tangent portfolio and σ_p^2 is its variance.

- Factor Model

$$r_i = E(r_i) + \beta_{i1}F_1 + \beta_{i2}F_2 + \dots + \beta_{ik}F_k + e_i$$

$$E(r_i) = r_f + \lambda_1\beta_{i1} + \lambda_2\beta_{i2} \dots + \lambda_k\beta_{ik}$$

- Convexity

Defintion of Convexity: $Convexity = \frac{1}{P * (1+y)^2} \sum_{t=1}^n [\frac{CF_t}{(1+y)^t} (t^2 + t)]$

Correction for Convexity: $\frac{\Delta P}{P} = -D_{MOD} * \Delta y + \frac{1}{2} [Convexity * (\Delta y)^2]$

- Summation of geometric series

$$\frac{1}{1+r} + \frac{1}{(1+r)^2} \dots + \frac{1}{(1+r)^n} = \frac{(1+r)^n - 1}{r(1+r)^n} \text{ for } -1 < r < 1$$

- Black Scholes

Formula for call and put options without dividends

$$C_0 = S_0 N(d_1) - X e^{-rT} N(d_2)$$

$$P_0 = X e^{-rT} [1 - N(d_2)] - S_0 [1 - N(d_1)]$$

$$d_1 = [\ln(S_0 / X) + (r + \sigma^2 / 2)T] / \sigma T^{1/2}$$

$$d_2 = d_1 - (\sigma T^{1/2})$$

Formula for call and put options with dividend yield of d

$$C_0 = S_0 e^{-dT} N(d_1) - X e^{-rT} N(d_2)$$

$$P_0 = X e^{-rT} [1 - N(d_2)] - S_0 e^{-dT} [1 - N(d_1)]$$

$$d_1 = [\ln(S_0 / X) + (r - d + \sigma^2 / 2)T] / \sigma T^{1/2}$$

$$d_2 = d_1 - (\sigma T^{1/2})$$

Formula for a warrant for m shares with n outstanding. Warrant price, W , solves equation:

$$W - \frac{n}{n+m} C_{BS}(S + \frac{mW}{n}, X, r, T) = 0$$

Tables of the Standard Normal Distribution



Probability Content from $-\infty$ to Z

z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990