Competitive Equilibrium Fraud in Markets for Credence-Goods

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7th October 2019

Abstract

This is a study of the nature and prevalence of persistent fraud in competitive markets for credence-quality goods. We model the market as a stochastic game of incomplete information in which the players are customers and suppliers and analyze their equilibrium behavior. Customers characteristics, search cost and discount rate, are private information. Customers do not possess the expertise necessary to assess the service they need either ex ante or ex post. We show that there exists no fraud-free equilibrium in the markets for credence-quality goods and that fraud is a prevalent and persistent equilibrium phenomenon.

Keywords: Competitve equilibrium fraud; Credence-quality goods markets; Search with learning;

^{*}Johns Hopkins University. We are grateful to Asher Wolinsky, Eilon Solan and Ehud Lehrer for their useful comments and suggestions.

1 Introduction

1.1 Motivation

There are markets in which customers seeking to purchase services that involve specialized knowledge might be defrauded by suppliers who prescribe unnecessary services. Examples include, medical tests and treatments, auto repairs, equipment maintenance, and taxi cab service. In these markets the service suppliers make diagnostic determinations of the service required and offer to provide it, and the customers must decide whether to purchase the prescribed service or to seek, at a cost, a second service prescription. Typically in these situations, the customer can judge, ex post, whether or not the service provided was *sufficient* to solving the problem, but is unable to assess whether the prescribed service was also *necessary*.

Darby and Karni (1973) were the first to identify the fundamental ingredients of the problem underlying the provision of what they dubbed *credence-quality goods*. First, information asymmetry between the customer who lacks the expertise required to assess the service needed and service provider who possess the required expertise and, second, the cost saving of the joint provision of diagnosis and services. This bundling of information and service is crucial.¹ They proceeded to discuss and analyze the economic implications of transactions involving this type of asymmetric information. Specifically, Darby and Karni argued that in competitive market equilibrium for credence-quality goods there is persistent tendency of suppliers to over-prescribe services (that is, to prescribe services that are sufficient but are not

¹See Wolinsky (1993) for an analysis of the implication of separation of diagnosis and service.

necessary to solve the problem at hand).

It is quite obvious that the fraud committed depends on the specific characteristics of the credence-good market. For example, the demand for auto-repair at a given service station depends on the waiting time (that is, the length of the queue) which may not be an issue when it comes to taxi cab service. It will also depend on the information the customer may acquire before choosing the service provider and the cost of searching for a second opinion. For instance, in some cases medical diagnosis may only be possible with invasive procedure, which makes the cost of obtaining a second opinion prohibitively high. In view of these observations, it seems obvious that modeling of credence goods markets, while incorporating the fundamental ingredients of the problem – information asymmetry and bundling of the diagnosis and service – must be based on specifics of the market under consideration. In this paper we focus on markets for the provision of services (for example, mechanical and medical services) in which the capacity of the service suppliers may result in waiting time for service. We underscore this point to avoid the impression that this is a general model of credence good markets. However, the we believe that the game-theoretic approach invoked here is quite general and is not specific to the analysis of the model we study in this paper.

Since the publication of Darby and Karni (1973), numerous studies confirm the prevalence of fraudulent behavior in the markets for credence-quality goods.² For medical services, especially physicians' services, over treatment, a phenomenon known in medical literature as supplier induced demand, is widely documented (see

 $^{^2\}mathrm{Dulleck}$ and Kerschbamer (2006) includes a survey of the literature and provides numerous references.

McGuire [2000], Currie, et. al [2011], Dranove [1988]). Domenighetti (1993) found that in Swiss canton of Ticino on average the population has one third more operations than medical doctors and their relatives, suggesting that greater information symmetry tends to reduce overprescription of surgical procedures. The same type of conclusion was reached by Balafoutas et. al. (2013). They report the results of a natural field experiment on taxi rides in Athens, Greece, designed to measure different types of fraud and to examine the influence of passengers' presumed information and income on the extent of fraud. Their findings indicate that passengers with inferior information about optimal routes are taken on significantly longer detours. Iizuka (2007) finds physicians drugs prescriptions are influenced by markup. Schneider (2012) reports the results of a field experiment designed to assess the accuracy of service provision in the auto repair market. He finds evidence for over prescription of services as well as under prescription. Beck et. al (2014) reports that in experimental setting, car mechanics are significantly more prone to supplying unnecessary services than student subjects.

The work of Darby and Karni, while calling attention to a neglected aspect of economic interactions that results in market failure, lacks the formal structure necessary to derive more subtle implications of the concept they introduced.³ In this work we take a step towards a more formal analysis of competitive markets for credence-quality services. Specifically, taking a game-theoretic approach, we analyze

³Theirs was the first paper after the seminal work of Akelof (1970) to discuss market failure due to asymmetric information. Unlike the asymmetry concerning hidden characteristics giving rise to adverse selection problem pointed out by Akerlof, the information asymmetry that concerns Darby and Karni has to do with the ability to assess the service needed which, in conjunction with the provision of service, gives rise to fraud.

the equilibrium behavior in a market in which two suppliers operating service stations are engaged in Bertrand competition. The suppliers are assumed to be ex ante identical in every respect and that the only asymmetry between them is the lengths of their queues, which arises endogenously. The suppliers post prices per service hour. We assume that Bertrand competition forces the price per service hour to be the same across suppliers.⁴ The critical aspect of the model is the information asymmetry regarding the service necessary to address the problem at hand. We assume throughout that the suppliers possess the expertise necessary to assess the required service while the customers do not.

Customers heterogeneity is the consequence of idiosyncratic cost of obtaining a second prescription and the cost of waiting for service, which depends on the length of the suppliers' queues. We assume that these costs are the customers' private information and that the customers discover the lengths of the suppliers queues only when they visit their service station.

We study the market in stationary equilibrium in which normal profits discourage entry or exit. In other words, the idle time at the service stations is short enough so that no supplier loses money but is sufficiently long so as to discourage new entries. We show that there exists no fraud-free competitive equilibrium in the credence good market, and that the level of fraud committed by the two suppliers depends on the lengths of their queues.

⁴The presumption is that the prices are posted and observed at no cost by all customers.

1.2 Related literature

Despite evidence regarding the prevalence of fraud in the market for credence goods and the distinguishing features of these markets, the theoretical literature dealing with the modeling and analysis of these markets is rather scant. The attempts to model competitive markets for credence-quality goods offer a variety of approaches. The works that are closest to ours in terms of the questions asked, are Wolinsky (1995), Emons (1997) and Dulleck and Kerschbamer (2006). Despite the shared interest in studying the prevalence of fraud in competitive equilibrium, these works are quite different from ours in the way they model the markets and, consequently, the equilibrium behavior of the customers and the suppliers.

Wolinsky (1995) proposed a model in which there are two states of disrepair, high and low. Customers do not possess the expertise necessary to determine the state and must relay on the diagnosis of the service providers. Wolinsky modeled the situation as a game in which the customers bargain with suppliers by offering a price for the repair. Suppliers have the option of rejecting the price, in which case the customers may increase their price or seek another supplier. Wolinsky showed that, in interior equilibrium, all customers who receive a prescription of the high service seek a second opinion, and the suppliers commit fraud by employing a strategy that assigns positive probability of rejecting price offers when the state diagnosed requires low service. This strategy reflects their belief that, to avoid the search cost, the customer may offer a higher price rather than seek a second opinion. Wolinsky's work is different from ours in the way the credence-goods markets are modeled and the conclusion of the analysis. To begin with, we allow for any number of states of disrepair measured by the service hours needed to resolve the problem. More importantly, we assume that the price of service hour are fixed by the suppliers (no bargaining) and is equal among the suppliers due to competition. Suppliers are characterized by the lengths of their queue and customers are characterized by their idiosyncratic search cost and discount rate. Customers are engaged in search with learning. These differences in modeling mandate different equilibrium notions and analysis.

Emons (1997) proposed a different model of credence good market in which the suppliers must decide whether to enter the market. If a supplier enters the market he is endowed with a fixed capacity that can be allocated to diagnosis and repair service. These two functions are assumed to be priced differently. The suppliers are allowed to announce a wrong diagnosis if they find that it is more profitable, for lack of capacity, to avoid providing the needed repair. The customers are identical. Emons studies conditions under which fraud free equilibrium exists. Emons model is different from ours in the specification of the information structure and the features of the credence-good market. These differences have implications for the depiction of the product state of disrepair; the characterization of the customers and their behavior; the pricing mechanism in the market; the suppliers strategies and the penalty imposed on them for not prescribing the necessary service.

Dulleck and Kerschbamer (2006) consider a market for credence services in which the customers may experience a need for high or low levels of service. They used a game theoretic approach to study conditions under which competition will eliminate fraud. These conditions include homogeneous customer population, cost conditions that prevent customers from seeking a second opinion and verifiability of the service provided. They discuss the implications of relaxing each of these conditions.

Less related theoretical models of the credence good market emphasized different aspects of the efficiency loss due to the asymmetric information. Hu and Lin (2018), Fong and Liu (2016) and Fong et. al (2017) study this issue in the context of interaction between uniformed customers and a monopolistic expert service provider and Heinzel (2019) study the equilibrium of a price-regulated market in which physicians characterized by heterogeneous cost compete for servicing uniformed patients. Hu and Lin modeled repeated interaction between a customer in occasional need of maintenance service of a durable good and a monopoly supplier. The optimal service required is of credence quality. Their analysis focuses on possible deviations from the optimal level of service by prescribing undertreatment or over treatment. They show that there exist no equilibrium that supports truthful diagnosis. Fong and Liu (2016) investigated the effect of liability on the seller's incentive to maintain good reputation and its impact on market efficiency. Fong et. al (2017) focus on the use of customer service to build trust between the monopoly supplier its customers so as to mitigate the efficiency loss. Heinzel models the interaction among physicians and patients as a game in which patients may employ mixed strategies in seeking "second opinion" when diagnosed as having a serious problem and physicians may defraud their patients by overtreating them for minor problems. Unlike in the model we present here, the distinct physicians' types is exogenous and the customer behavior is not derived from optimal search strategy.

In the next section we describe the credence good market. The equilibrium ana-

lysis appears in section 3. Some economic implications of our analysis are discussed in section 4. Section 5 includes a discussion of our results. To allow for uninterrupted reading we collected the proofs of the main results in section 6.

2 The Credence Good Market

2.1 Overview

Consider a market for a credence-quality service populated by customers and two service suppliers, A and B. The information asymmetry in this market is two sided. The customers' private information consists of their idiosyncratic search cost and discount rate. The suppliers possess expertise that the customers do not have, which allows them to observe the actual state of disrepair and assess the service needed to fix the problem. Let $\tilde{\omega}$ denote the discrete random variable representing the true state of disrepair expressed as the necessary and sufficient number of service hours required to address the problem. We normalize $\tilde{\omega}$ to take values in $\Omega := \{\omega_1, ..., \omega_n\}$, where $0 < \omega_1 < < \omega_n < 1.5$ Denote the distribution of $\tilde{\omega}$ by $\mu \in \Delta(\Omega)$, where $\Delta(\Omega)$ denotes the simplex in \mathbb{R}^n . We assume that μ is exogenous and commonly known. We also assume throughout that the prescribed service must fix the problem (malfunction, malaise) or the customer refuses payment. Since the set of states Ω is common knowledge, the prescribed service must correspond to the states and be at least as large as the minimal service required to address the problem (that is,

⁵As will become clear later, the assumption of discrete state space has implications for the customers perception of the difference between the suppliers strategies.

if the state is ω_i then $q \in {\omega_i, ..., \omega_n}$.⁶ The two suppliers are identical in every respect except for the lengths of their queues, expressed in terms of service hours committed to serving customers in the queues. We assume that the suppliers observe each other's queue and that customers only discover the length (waiting time for service) of a supplier's queue upon visiting the supplier.⁷ Let $Q^A(t)$ and $Q^B(t)$ denote the lengths of the suppliers queues at time t and suppose that the market is such that the lengths of the queues are bounded by the market size, \bar{Q} .⁸ Formally, $(Q^A(t), Q^B(t)) \in I := \{(Q^A(t), Q^B(t)) \in \mathbb{R}^2_+ | Q^A(t) + Q^B(t) \leq \bar{Q}\}$, for all t. Then, at each interaction, the credence-quality service market is parametrized by a state depicted by the triplet $(\omega, Q^A(t), Q^B(t)) \in \Omega \times I$. It is important to keep in mind that prior to visiting a supplier, the customers do not know the state. Consequently, from the customers' ex ante point of view, the two suppliers are identical.

We model the credence service market as a stochastic game of incomplete information, denoted Γ . We assume that new customers arrive at random times, following some underlying stochastic process. A customer's arrival on the market at time t in state of disrepair ω when the suppliers queues are $Q^A(t)$ and $Q^B(t)$ initiates a dynamic *stage game*, $\Gamma(\omega, Q^A(t), Q^B(t))$, depicting the interaction among the customer and the two suppliers. When a new customer shows up at a service

⁶This assumption is dubbed liability in the literature (see Dulleck and Kreschbamer [2006], Fong an Liu [2016] and Fong et al. [2017]).

⁷The assumption that the suppliers observe each other's queue expresses the presumption that survival in a competitive market requires the players to keep tab of their rivals positions and actions. Relaxing this assumption would require a modification of the suppliers strategies described below, and will complicate the analysis without providing new insights.

⁸This assumption corresponds to the empirical fact that market sizes are finite. From the analytical point of view this assumption implies the compactness of the domain of the joint distribution of the lengths of the queues.

station, the supplier observes the state of disrepair ω and, consequently, the state $(\omega, Q^A(t), Q^B(t))$. The suppliers do not observe the customer's type. Customers know their types but not the state of disrepair ω . They discover the length of a supplier's queue upon visiting a service station and receiving a diagnosis. In other words, a customer may discover the lengths of the suppliers queues sequentially, during the process of searching for service. Insofar as the customers are concerned, what matters are the lengths of the queues and not the identity of the suppliers. This assumption rules out suppliers' identity or reputation as a possible factor.⁹

At a state $s(t, \omega) := (\omega, Q^A(t), Q^B(t))$ the suppliers and customers make their decisions following which the game proceeds to the next state as follows. Suppose that the next customer arrives at time t' in a state of disrepair ω' . Let $\Delta t' := t' - t$. If the customer that arrives at time t' accepts the prescription q^A of supplier A then the new state is

$$s_{A}(t',\omega') := \left(\omega', \max\{Q^{A}(t) - \Delta t' + q^{A}, 0 + q^{A}\}, \max\{Q^{B}(t) - \Delta t', 0\}\right),\$$

and if she accepts the prescription q^B of supplier B then the new state is

$$s_B(t',\omega') := \left(\omega', \max\{Q^A(t) - \Delta t', 0\}, \max\{Q^B(t) - \Delta t' + q^B, 0 + q^B\}\right).$$

The transition probability from the state $s(t, \omega)$ to the state $s_j(t', \omega')$, denoted $\rho(s(t, \omega), s_j(t', \omega')), j \in \{A, B\}$, is the product of the probability $\mu(\omega')$ that the state of disrepair is ω' ; the probability that supplier j prescribes q^j in equilibrium;

⁹We revisit the issue of reputation in the discussion section.

the probability that the newly arrived customer, employing the equilibrium search strategy, accepts the prescription q^{j} . A detailed exposition of these probabilities and the induced stochastic evolution of the queues are developed in Section 3 below.

2.2 The customers

A customer's type, (θ, β) , consists of idiosyncratic search cost, θ , and discount rate, β , both taking values in [0, 1]. Thus, the set of customers' types is $T = [0, 1]^2$. Let $\mathcal{B}(T)$ be the Borel sigma algebra on T and denote by ξ a continuous probability measure on the measurable type space $(T, \mathcal{B}(T))$.

Upon identifying an equipment malfunction or a sense of malaise indicating, respectively, potential mechanical or health problem, the customer engages in sequential search for repair service or medical treatment. Diagnosis of the problem and determination of the service, or treatment, needed to resolve it requires expert knowledge, which the customer does not possess.

The customers' strategies: We assume that the customer chooses one of the two service outlets at random with equal probabilities.¹⁰ Upon visiting a service outlet the customer obtains a service prescription, expressed in terms of service-hours, and the information regarding the waiting time for the service delivery (that is, the length of the queue at that service station). The customer must then choose between accepting the prescribed service and waiting in the queue and rejecting it in favor of seeking a second prescription. If she decides to obtain a second opinion, the

¹⁰This assumption does not rule out customers loyalty to suppliers or that each customer visits first the supplier whose location is closer provided that the loyalty or proximity are equally devided between the suppliers.

customer visits the second supplier, receives a second prescription and observes the length of the supplier's queue. The customer must then decide whether to accept the second prescription or return to the first supplier. We assume that the search is with recall. Hence, if the customer decides to seek a second prescription and then return to the first supplier, she maintains her place in the queue and is entitled to obtain the service prescribed by the first supplier. However, returning to the first supplier after visiting the second entails a cost, expressed as utility loss.

Formally, a customer's search strategy is a mapping $\sigma : T \to \Sigma_1 \times \Sigma_2$, where $\Sigma_1 := \{\sigma_1 : \Omega \times I \to \{0,1\}\}, \Sigma_2 := \{\sigma_2 : \Omega^2 \times I \times K(Q_1) \to \{0,1\}\}$, where $K(Q_1) := \{Q \in \mathbb{R}_+ \mid Q \leq \overline{Q} - Q_1\}$. In other words, the strategy assigns to a customer of type (θ, β) two acts depicted by the functions $\sigma_1^{(\theta,\beta)} : \Omega \times I \to \{0,1\}$ and $\sigma_2^{(\theta,\beta)} : \Omega^2 \times I \times K(Q_1) \to \{0,1\}$, where $\sigma_1^{(\theta,\beta)}(q_1,Q_1) = 1$ means that the customer accepts the prescription of the first supplier she visits and terminates the search, and $\sigma_1^{(\theta,\beta)}(q_1,Q_1) = 0$ means that she seeks a second prescription. Similarly, $\sigma_2^{(\theta,\beta)}(q_2,Q_2;q_1,Q_1) = 1$ means that the customer accepts the second supplier's prescription and $\sigma_2^{(\theta,\beta)}(q_2,Q_2;q_1,Q_1) = 0$ means that she rejects the second supplier's prescription and return to the first supplier. We denote by Σ the set of customers' strategies.

The customers' beliefs: Since the customers do not observe the suppliers queues, at the outset the customer's information set is $\Omega \times I^2$ and her prior beliefs are captured by the commonly known distributions μ on Ω and v on I^2 . Upon observing the length of the queue, Q_1 , and obtaining a prescription, $q_1 \in \Omega$, from the the first supplier, the customer updates her beliefs about the prescription she will receive from the second supplier and the waiting time at the second service station. In doing so, the customer is supposed to apply Bayes rule.¹¹ The updated beliefs, regarding the second supplier's queue conditional on the first supplier' prescription, q_1 and Q_1 , is represented by the conditional distribution $m(q_2, Q_2 \mid q_1, Q_1)$ on $\Omega \times I \times K(Q_1)$.¹²

The customers' payoffs: Accepting a prescribed service q on her first visit from a supplier whose queue length is Q, the utility from fixing the problem to a customer of type (θ, β) is: $u^{\beta}(q, Q) = w(q) e^{-\beta Q}$, where w is monotone decreasing and differentiable function. Without loss of generality, we assume that $w(\omega_1) = 1$ and $w(\omega_n) = 0$. Continuing the search entails a customer-specific search cost, $\theta \in [0, 1]$, expressed as utility discount. Thus, the utility of accepting the prescription, q' when the queue of the second supplier is Q' is $u^{(\theta,\beta)}(q',Q') = \theta w(q') e^{-\beta Q'}$. Returning to the first supplier after visiting the second supplier, the customer's payoff is $\theta^2 w(q) e^{-\beta Q}$.

2.3 The suppliers

There are two suppliers, A and B, operating identical service outlets, engaged in Bertrand competition. Assume that the hourly cost of operating a service outlet is c > 0, regardless of whether the service station is occupied. The profit generated by servicing customers for a fraction, x, of an hour is: $\pi(x) = xp - c$, where p denotes the price per hour of service. Let $\bar{x} \in [0, 1]$ denote the average fraction of an hour the service station is occupied.¹³

Assuming free entry and exit, the stability of the market with two suppliers is based on the implicit assumption that both suppliers provide, on average, sufficient

¹¹This is the sense in which the search involves learning.

¹²We examine the updated beliefs in further details below.

¹³If the provision of service involves additional variable costs, say xc_v , then the profit is $\pi(x) = x(p-c_v) - v$. This reformation does not affect the analysis that follows.

number of service hours per period to earn normal profit, so that there is no incentive for new suppliers to enter the market or for a current supplier to exit the market. Formally, the long-run stability of the market requires that the price is such that $\pi(\bar{x}) = \bar{x}p - c = 0.$

The suppliers' strategies: At every point each supplier has a queue representing hours committed to serving customers that have already accepted the supplier's prescriptions. The length of the queues are determined by the history of customer arrivals, their service prescriptions, and their acceptance decisions. In other words, the lengths of the queues are determined by the realization of an exogenous stochastic process (that is, the arrival rate and the random state $\tilde{\omega}$) and the endogenous decisions of the suppliers and customers.

The suppliers' prescription mixed strategies are mappings $G: \Omega \times I^2 \to \mathcal{G}$, where \mathcal{G} denotes the set of CDF on Ω .¹⁴ Formally, for each $q_k \in \Omega$ and $(Q^j, Q^{-j}) \in I^2$, $G(\omega, Q^j, Q^{-j}) := \Sigma_{i=1}^k g(\omega, Q^j, Q^{-j})(q_i) \, \delta_{q_i}$, where $(g(\omega, Q^j, Q^{-j})(q_1), ..., g(\omega, Q^j, Q^{-j})(q_n)) \in$ $\Delta(\Omega), j \in \{A, B\}$ and δ_{q_i} denotes the distribution function that assigns the unit probability mass to q_i . Henceforth, when there is no risk of misunderstanding, we suppress the state and write $g(\cdot)$ instead of $g(\omega, Q^j, Q^{-j})(\cdot)$ and use $G(\omega, Q^j, Q^{-j})$ and $g(\omega, Q^j, Q^{-j})$ interchangeably to designate the suppliers' strategies. Since the only asymmetry between the suppliers is due to the lengths of their queues, the suppliers strategies are distinct only as a result of the relative lengths of their queues.

The suppliers' payoffs: Consider supplier j's, $j \in \{A, B\}$, problem when a new customer shows up at time t in state ω when the queues are Q^A and Q^B ,

¹⁴We are restricting consideration to history-independent, or Markovian, strategies.

thereby initiating the stage game $\Gamma(\omega, Q^A, Q^B)$. Denote by \tilde{t} the random waiting time for the arrival of the next customer taking values in \mathbb{R}_{++} . Let F denote the CDF of \tilde{t} and assume that it is time independent and has full support. Denote by $\alpha_j (q_j \mid Q^A, Q^B, \omega_i, \sigma, q_{-j})$ the probability that supplier j's prescription, q_j , be accepted conditional on the rival's prescription q_{-j} and the customer's strategy, σ . Then, the probability that supplier j's prescription, q_j , is accepted conditional on the rival's and customer's strategies, G^{-j} and σ , respectively, is $\alpha_j (q_j \mid Q^A, Q^B, \omega_i, \sigma, G^{-j}) =$ $\Sigma_{q \in \Omega_{\omega_i}} \alpha_j (q_j \mid Q^A, Q^B, \omega_i, \sigma, q) g^{-j} (q)$. A more detailed and formal discussion of these probabilities appear in section 3.2 below.

Consider the situation at time t. Looking ahead, the suppliers anticipate serving the customers in the queues while waiting for the next customer to show up. Without loss of generality, let t = 0 be the present time and let $Q^j = Q^j(0)$, and $\Delta t' = t'$ for $t' \ge 0$. Let Q^j , $j \in \{A, B\}$, denote the length of the queue of supplier j at t = 0. Define the *interim value functions* $v_j : I^2 \times \Omega^2 \times \mathbb{R}_+ \to \mathbb{R}, j \in \{A, B\}$, as follows: Let

$$\psi\left(t' \mid Q^{j}\right) = \begin{cases} e^{-rt'} & \text{if } t' \leq Q^{j} \\ 0 & \text{if } t' > Q^{j} \end{cases}$$
$$\left(Q^{A}, Q^{B}, \omega_{i}, q_{j}, t'\right) = (1 - \alpha_{j} \left(q_{j} \mid G^{-j}, \sigma\right))\psi\left(t' \mid Q^{j}\right) + \alpha_{j} \left(q_{j} \mid G^{-j}, \sigma\right)\psi\left(t' \mid Q^{j} + q_{j}\right)$$
$$(1)$$

where r > 0 denotes the discount rate.

 v^j

Denote by $V^j: \Omega \times I^2 \times \Omega \to \mathbb{R}$ supplier j's continuation value function (that is, the discounted expected value given the strategies (G, σ)). Then supplier j's objective is to choose a strategy $G \in \mathcal{G}$ that is best response to the rival's and the customer's strategies.¹⁵ Formally,

$$\max_{G \in \mathcal{G}} \sum_{q \in \Omega_{\omega_i}} \left[\int_0^\infty \left[v^j \left(Q^A, Q^B, \omega_i, q, t' \right) + e^{-rt'} \sum_{\omega \in \Omega} V^j \left(\omega, Q^A(t'), Q^B(t'), q \right) \mu(\omega) \right] dF(t') \right] g(q)$$

$$\tag{2}$$

where $\Omega_{\omega i} := \{\omega_i, \omega_i + 1, ..., \omega_n\}$ and

$$V^{j}\left(\omega_{i},Q^{j}(t'),Q^{-j}\left(t'\right),q_{j}\right) =$$

$$\alpha_{j}\left(q_{j} \mid G^{-j}, \sigma\right) V^{j}\left(\max\{Q^{j} - t' + q_{j}, 0\}, \max\{Q^{-j} - t', 0\}, \omega\right) +$$
(3)

 $\Sigma_{q \in \Omega_{\omega_{i}}} V^{j} \left(\max\{Q^{j} - t', 0\}, \max\{Q^{-j} + q - t', 0\}, \omega \right) \alpha_{-j} \left(q \mid Q^{A}, Q^{B}, \omega, \sigma, q_{j} \right) g^{-j} \left(q \right).$

 $j \in \{A, B\}.$

Clearly, $V^{j}(\omega, Q^{A}, Q^{B})$, $j \in \{A, B\}$ is strictly monotonic increasing function of the supplier's own queue length. Furthermore, regardless of the length of their queues, supplier A's payoff satisfies $V^{A}(\omega, Q^{A} + q, Q^{B}) > V^{A}(\omega, Q^{A}, Q^{B} + q)$ and supplier \dot{B} 's payoff satisfies $V^{B}(\omega, Q^{A} + q, Q^{B}) < V^{B}(\omega, Q^{A}, Q^{B} + q)$.

3 Equilibrium Analysis

3.1 Equilibrium defined

We analyze the credence service market as a stochastic game of incomplete information invoking the concept of sequential equilibrium. At the start the customers learn

¹⁵Further discussion of the continuation value function appears in Section 3.2.2 below.

their types. However, when customers detect a problems and seek remedial service, they do not know which particular stage game $\Gamma(\omega, Q^A, Q^B)$ is being played.

The suppliers observe each other's queue and, when a customer calls, they observe the state ω . However, the suppliers do not observe the customer's type. Consequently, even though at each stage game the suppliers face a single customer, not knowing the customer's type, the suppliers play strategies that are best responses against the average acceptance probability of the customer population of types induced by σ . To understand the customers' acceptance probabilities we need to understand the evolution of the customers beliefs.

The customer's system of beliefs $\eta := (\mu, v, m(\omega, Q_2 | q_1, Q_1))$ consists of the prior belief about the stage game being played, determined by the prior beliefs μ on Ω and v on I^2 , and the updated beliefs $m(\omega, Q_2 | q_1, Q_1)$ on $\Omega \times I$. To simplify the notation, when there is no risk of confusion, we write G^j instead of $G(\omega_i, Q^j, Q^{-j})$, $j \in \{A, B\}$. A strategy profile (σ, G^A, G^B) , is sequentially rational if, given the suppliers objective functions, G^A is best response against (σ, G^A) , G^B is best response against (σ, G^A) , and σ is best response against (G^A, G^B) , for all $(\omega, Q^A, Q^B) \in \Omega \times I^2$. A Markovian equilibrium is a strategy-profile (σ, G^A, G^B) that is sequentially rational given the system of beliefs η . Given $\omega_i \in \Omega$, a strategy G_k is completely mixed with modulus k if $g_k(q) \ge k^{-1}$, for all $q \in \Omega_{\omega_i}$.

Definition 1: A point $(\hat{V}^A, \hat{V}^B, \hat{G}^A, \hat{G}^B, \hat{\sigma})$ and a system of beliefs η^* constitute a Markovian sequential equilibrium of the stochastic game induced by the credence good market if:

(i) The strategy profile $(\hat{\sigma}, \hat{G}^A, \hat{G}^B)$ is sequentially rational given the belief sys-

tem $\eta^* = (\mu, v, m^*)$ and the value functions \hat{V}^A, \hat{V}^B .

(*ii*) There exist sequence of value functions and strategy profiles $\{(V_k^A, V_k^B, G_k^A, G_k^B, \sigma_k)\}_{k=1}^{\infty}$, where (G_k^A, G_k^B, σ_k) is a Markovian equilibrium in completely mixed strategies with modulus k of the credence good market game, with $\lim_{k\to\infty} (V_k^A, V_k^B, G_k^A, G_k^B, \sigma_k) =$ $(\hat{V}^A, \hat{V}^B, \hat{G}^A, \hat{G}^B, \hat{\sigma}), \eta^* = \lim_{k\to\infty} (\mu, v, m^k (q_2, Q_2 \mid q_1, Q_1)) \text{ and } m^k (q_2, Q_2 \mid q_1, Q_1)$ derived from the prior beliefs (μ, v) and strategy profile (G_k^A, G_k^B, σ_k) using Bayes' rule and, for $j \in \{A, B\}$,

$$V_{k}^{j} = \max_{G_{k}\in\mathcal{G}_{k}}\sum_{q\in\Omega_{\omega_{i}}}\left[\int_{0}^{\infty}\left[v_{k}^{j}\left(Q^{A},Q^{B},\omega_{i},q,t'\right) + e^{-rt'}\sum_{\omega\in\Omega}V_{k}^{j}\left(\omega,Q^{A}(t'),Q^{B}(t'),q\right)\mu\left(\omega\right)\right]dF\left(t'\right)\right]\hat{g}_{k}^{j}\left(q\right).$$

3.2 Equilibrium: Existence

We turn next to the study of the existence of Markovian sequential equilibrium of the credence good market game Γ . We begin by examining the behavior of the customers and the suppliers. We assume that when a new customer arrives the supplier does not know whether he is the customer's first or second call. The supplier diagnoses the problem (that is, the supplier observes the state ω) and prescribes a service, $q \in \Omega_{\omega}$. The supplier also informs the customer the waiting time for service, which is equals to the length of the supplier's queue, Q.

3.2.1 The customers

The customers system of beliefs: The customers prior beliefs are depicted by the distributions $\mu \in \Delta(\Omega)$ and v on I^2 , which are assumed to be commonly known. Moreover, in view of the ex ante symmetry of the suppliers, insofar as the customers are concerned, v be symmetric.

Consider the state (ω, Q^A, Q^B) and let $G_k^j(\omega, Q^A, Q^B)$, $j \in \{A, B\}$, be the (mixed) strategies of the suppliers. The customers are supposed to know the strategies of the suppliers as functions of the states but not the current state (ω, Q^A, Q^B) and stage game $\Gamma(\omega, Q^A, Q^B)$. In particular, the customers do not know which is the short-queue supplier and which is the long-queue supplier. Let (q_1, Q_1) and (q_2, Q_2) denote the prescriptions obtained and queues observed by a customer in her first and second visits, respectively.

Following her visit to the first supplier, regardless of whether it is A or B, and having observed Q_1 the customer deduces, for every Q_2 , whether it is shorter or longer than Q_1 . The customer updates her beliefs about the state of disrepair, ω , and the length of the queue of the second supplier by applying Bayes' rule as follows: For all $\omega_i \leq q_1$,

$$m^{k}(\omega_{i}, Q_{2} \mid q_{1}, Q_{1}) = \begin{pmatrix} \frac{g_{k}(\omega_{i}, Q_{1}, Q_{2})(q_{1})\mu(\omega_{i})v(Q_{2}, Q_{1})}{\int_{Q_{1}}^{\infty} [\Sigma_{\omega_{1} \leq \omega_{i} \leq q_{1}}g_{k}(\omega_{i}, Q_{1}, Q)(q_{1})\mu(\omega_{i})]dv(Q, Q_{1})} & \text{if } Q_{2} \geq Q_{1} \\ \frac{g_{k}(\omega_{i}, Q_{1}, Q_{2})(q_{1})\mu(\omega_{i})v(Q_{2}, Q_{1})}{\int_{0}^{Q_{1}} [\Sigma_{\omega_{1} \leq \omega_{i} \leq q_{1}}g_{k}(\omega_{i}, Q_{1}, Q)(q_{1})\mu(\omega_{i})]dv(Q, Q_{1})} & \text{if } Q_{2} < Q_{1} \end{pmatrix}, \quad (4)$$

where $g_k(\omega_i, Q_1, Q_2)$ is the mixed strategy of the second supplier.¹⁶

The customers expected payoff and best response strategies: We explore next the optimal behavior of the customer in the subgame following her visit to the first supplier and the evolution of her beliefs. Having obtained the prescription q_1 and observing the length of the queue, Q_1 , a customer of type (θ, β) can accept the

¹⁶This assumption entails, implicitly, that the suppliers' names are uniformative (that is to say, from an ex ante point of view they are symmetric).

prescription and stop the search or seek a second prescription. In the latter case the customer accepts the second supplier's prescription if $u^{\beta}(q_2, Q_2) \ge \theta u^{\beta}(q_1, Q_1)$. Otherwise the customer exercises the recall option and returns to the first supplier to obtain the payoff $\theta^2 u^{\beta}(q_1, Q_1)$.

Because in her the second visit the customer is going to accept or reject the second offer according to whether $u^{\beta}(q_2, Q_2)$ is greater or smaller than $\theta u^{\beta}(q_1, Q_1)$, given q_1 and Q_1 the reservation utility of a customer of type (θ, β) , $u_r^{(\theta, \beta)}(q_1, Q_1)$, is given by

$$u_{r,k}^{(\theta,\beta)}(q_1,Q_1) =$$
 (5)

$$\Sigma_{\omega_{1} \leq \omega_{h} \leq q_{1}} \Sigma_{\omega_{h} \leq q_{2} \leq \omega_{n}} \left[\int_{0}^{Q_{1}} \max\{\theta u^{\beta}(q_{2}, Q_{2}), \theta^{2} u^{\beta}(q_{1}, Q_{1}))\} g_{k}(q_{2}) m^{k}(\omega_{h}, Q_{2} \mid q_{1}, Q_{1}) dQ_{2} \right]$$
$$+ \int_{Q_{1}}^{\infty} \max\{\theta u^{\beta}(q_{2}, Q_{2}), \theta^{2} u^{\beta}(q_{1}, Q_{1}))\} g_{k}(q_{2}) m^{k}(\omega_{h}, Q_{2} \mid q_{1}, Q_{1}) dQ_{2} \right],$$

where $g_k(\cdot) = g_k(\omega_i, Q_1, Q_2)(\cdot)$.

Given her type, (θ, β) , and the suppliers' strategy, G_k , the customer's expected payoff upon observing (q_1, Q_1) given the reservation utility $u_{r,k}^{(\theta,\beta)}(q_1, Q_1)$ in (5), is:

$$\bar{U}\left(\sigma_{k}\left(\theta,\beta\right),G_{k}^{A},G_{k}^{B}\right)=\sigma_{1,k}^{\left(\theta,\beta\right)}u^{\beta}\left(q_{1},Q_{1}\right)+\left(1-\sigma_{1}^{\left(\theta,\beta\right)}\right)u_{r,k}^{\left(\theta,\beta\right)}\left(q_{1},Q_{1}\right).$$
(6)

Hence, the customer accepts the first supplier's offer (that is, set $\sigma_{1,k}^{(\theta,\beta)} = 1$) if $u^{\beta}(q_1, Q_1) \ge u_{r,k}^{(\theta,\beta)}(q_1, Q_1)$. Otherwise, the customer continues the search (that is, set $\sigma_{1,k}^{(\theta,\beta)} = 0$). She accepts the second supplier's offer (that is, set $\sigma_{2,k}^{(\theta,\beta)} = 1$) if $u^{\beta}(q_2, Q_2) > \theta u^{\beta}(q_1, Q_1)$. Otherwise, she exercises the recall option (that is, set $\sigma_{2,k}^{(\beta,\theta)} = 0$). With this in mind we make the following definition:

Definition 2: A reservation-utility search strategy $\sigma_k : T \to \Sigma_1 \times \Sigma_2$ consists of two mappings $\sigma_{1,k}^{(\theta,\beta)} : \Omega \times I \to \{0,1\}$ and $\sigma_{2,k}^{(\theta,\beta)} : \Omega^2 \times I^2 \to \{0,1\}$, and a function $u_{r,k}^{(\theta,\beta)} : \Omega \times I \to [0,1]$ such that:

(a)
$$\sigma_{1,k}^{(\theta,\beta)}(q,Q) = 1$$
 if $u^{\beta}(q,Q) \ge u_{r,k}^{(\theta,\beta)}(q,Q)$ and $\sigma_{1,k}^{(\theta,\beta)}(q,Q) = 0$, otherwise.
(b) $\sigma_{2,k}^{(\theta,\beta)}(q_2,Q_2;q_1,Q_1) = 1$ if $\sigma_{1,k}^{(\theta,\beta)}(q_1,Q_1) = 0$ and $u^{\beta}(q_2,Q_2) > \theta u^{\beta}(q_1,Q_1)$
and $\sigma_{2,k}^{(\theta,\beta)}(q_2,Q_2;q_1,Q_1) = 0$, otherwise.

We summarize the above discussion in the following:

Proposition 1. A reservation-utility strategy is the customers' unique best response to the suppliers' strategy profile $(G_k^A(\omega, Q^A, Q^B), G_k^B(\omega, Q^A, Q^B))$, for all $(\omega, Q^A, Q^B) \in \Omega \times I^2$.

In view of Proposition 1, the reservation-utility strategy based on the reservationutility function $u_{r,k}^{(\theta,\beta)}(q_1,Q_1)$ is the best response strategy of the customers in the subgame following the visit to the first supplier.

Lemma 1: For each type $(\theta, \beta) \in T$ and all $(q_1, Q_1) \in \Omega \times I$ the customer's expected payoff, $\overline{U}(\sigma_k(\theta, \beta), G_k^A, G_k^B)$, of the reservation-utility strategy is continuous.

The continuity of \overline{U} is an immediate implication of its linearity in the strategies and the fact that $g_k^j(q) > 0, j \in \{A, B\}$, for all $q \in \Omega_{\omega}$.

3.2.2 The suppliers

Because the customer's type is private information, the suppliers must choose their strategies as best responses against the acceptance probabilities induced by the distribution of customers' types. We examine next the acceptance probabilities induced by reservation utility strategies. For $j \in \{A, B\}$, the supplier j's utility of subscribing q is $V^i (Q^j + q, Q^{-j})$ in the following cases: (1) supplier j is the customer's first call and the customer accepts the prescription q immediately, (2) supplier j is the customer's first call, the customer rejects supplier j's prescription in the first visit seeking a second prescription and returns to supplier j for the service, (3) supplier j is the customer's second call and she accepts his prescription. We calculate next the probabilities of these events.

The first-call suppliers face a distribution of acceptance rules induced by the distribution, ξ , on the set of types. Thus, for all $(q_1, Q_1) \in \Omega \times I$, the subset of the first callers who do not seek a second prescription when faced with the prescription q_1 and queue Q_1 is given by the subset of types $A_{1,k}(q_1, Q_1) := \{(\theta, \beta) \in T \mid u^\beta(q_1, Q_1) \geq u_{r,k}^{(\theta,\beta)}(q_1, Q_1)\} \in \mathcal{B}(T)$. Consequently, the average acceptance rate of first callers who, given the queue length Q_1 , accepts the prescription q_1 immediately is:

$$\sigma_{1,k}(q_1, Q_1) = \int_T \sigma_{1,k}^{(\theta,\beta)}(q_1, Q_1) \, d\xi(\theta,\beta) = \xi(A_{1,k}(q_1, Q_1)).$$

This may be interpreted as the *probabilistic demand* function of first callers.

Given the prescription q_1 and queue length Q_1 of the first supplier the customer happened to visit, the acceptance rate of a second prescription, q_2 , when the length of the queue of the second supplier is Q_2 , is:

$$\sigma_2(q_2, Q_2 \mid q_1, Q_1) = \int_T \sigma_2^{(\theta, \beta)}(q_2, Q_2; q_1, Q_1) d\xi(\theta, \beta).$$

The second-call supplier does not know that he is the second-call supplier and does not observe the first-call supplier's prescribed service. However, since q_1 is determined by the supplier's mixed strategy, observing ω_i and Q_1 , the second supplier can infer that, *if* he is the customer's second-call then the prescription the customer obtained in her first call is a random variable \tilde{q}_1 whose conditional probability distribution is determined by the strategy of the first supplier. Specifically, if the customer first visits supplier A then q_1 was determined by the strategy $G_k(\omega_i, Q^A, Q^B)$ and if the customer first visits supplier B then q_1 was determined by the strategy $G_k(\omega_i, Q^B, Q^A)$. Consequently, given (ω_i, Q^A, Q^B) , if j is the second supplier the customer calls upon, the probability that his prescribed service is accepted is

$$\varsigma_2\left(q^j,\omega_i,Q^j,Q^{-j},G_k\right) = \Sigma_{q\in\Omega_{\omega_i}}\sigma_2\left(q^j,Q^j\mid q,Q^{-j}\right)g_k\left(\omega_i,Q^{-j},Q^j\right)(q), \ j\in\{A,B\}.$$

Hence, the probability that a newly arrived customer accepts the prescription of supplier $j, j \in \{A, B\}$, is:

$$\alpha_{j}\left(q \mid \sigma, G_{k}\left(\omega_{i}, Q^{-j}, Q^{j}\right)\right) :=$$

$$\frac{1}{2} [\sigma_{1}\left(q, Q^{j}\right) + \left(1 - \sigma_{1}\left(q, Q^{j}\right)\right)\left(1 - \varsigma_{2}\left(q, \omega_{i}, Q^{j}, Q^{-j}, G_{k}(\omega_{i}, Q^{-j}, Q^{j})\right) + \Sigma_{q^{-j} \in \Omega_{\omega_{i}}}\left(1 - \sigma_{1}\left(q^{-j}, Q^{-j}\right)\right)\sigma_{2}\left(q, Q^{j} \mid q^{-j}, Q^{-j}\right)g_{k}\left(\omega_{i}, Q^{j}, Q^{-j}\right)\left(q^{-j}\right)],$$

$$(7)$$

Supplier j's payoff is:

$$\max_{g_k \in \cdot(\Omega)} \sum_{q \in \Omega_{\omega_i}} \left[\int_0^\infty [v^j \left(Q^A, Q^B, \omega_i, q \right) + e^{-rt'} \sum_{\omega \in \Omega} V^j \left(Q^A(t'), Q^B(t'), \omega_j \right) \mu(\omega)] dF(t') \right] g_k \left(\omega_i, Q^j, Q^{-j} \right) (q)$$
(8)

where

$$V^{j}\left(\omega_{i}, Q^{j}(t'), Q^{-j}(t'), q\right) = \alpha_{j}\left(q \mid \sigma, G_{k}\left(\omega_{i}, Q^{-j}, Q^{j}\right)\right)V^{j}\left(\omega_{i}, \max\{Q^{j} - t' + q, 0\}, \max\{Q^{-j} - t', 0\}\right) +$$
(9)

$$\Sigma_{q'_{\in\Omega_{\omega_i}}} V^j \left(\omega_i, \max\{Q^j - t', 0\}, \max\{Q^{-j} + q - t', 0\}\right) \times \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q'\right) + \alpha_{-j} \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) \left(q' \mid \sigma, G_k \left(\omega_i, Q^j, Q^{-j}\right)\right) g_k \left(Q^{-j}(t'), Q^j(t'), \omega_i\right) g_k \left(Q^{-j}(t'), Q^{-j}(t'), Q^{-j}(t')\right) g_k \left(Q^{-j}(t'), Q^{-$$

Lemma 2: For all $\omega, Q^A, Q^B \in \Omega \times I^2$, the expression (8) is a continuous function on the strategy profiles set $\Sigma \times \Delta(\Omega)^2$.

The proof appears in Section 6.1.

Our first result establishes the existence of Markovian sequential equilibrium of the stochastic game Γ .

Theorem 1: There exist Markovian sequential equilibrium of the stochastic game Γ induced by the credence good market.

To prove the theorem we begin by restricting the suppliers' strategies to be totally mixed. Specifically, we assume for some large $k \in N$ and all $q \in \Omega_{\omega_i}$ and $j \in \{A, B\}$, $g_k^j(\omega_i, Q^j, Q^{-j})(q) \geq \frac{1}{k}$ and prove the existence of Markov equilibrium. The proof involves the following steps: First, we prove that the players' objective functions are all continuous in respect to other players' strategies. The, invoking Berge maximum theorem, we conclude that the range of the correspondence that maps the set of value functions and strategies to itself is upper-semi continuous with range that is a convex-valued and compact set. Then, by Kakutani's theorem, we conclude that the aforementioned correspondence has fixed point. Second, we verify that the strategies corresponding to fixed points constitute a stationary Markov equilibrium and the value functions corresponding to the same fixed points are the equilibrium value functions. Third, taking the limits as k tends to infinity and invoking sequential compactness, we conclude that there exist convergent subsequence of fixed points and, hence, a limit point of fixed points. Finally, we invoke uniform continuity to show that such limit point is indeed an equilibrium point.

4 Fraudulent Behavior and Short-Queue Advantage

4.1 Fraud-free equilibrium

An equilibrium is said to be *fraud-free* if the equilibrium strategies, $\hat{G}(\omega_i, Q^j, Q^{-j}) = \delta_{\omega_i}$, for $j \in \{A, B\}$ for all $(\omega_i, Q^j, Q^{-j}) \in \Omega \times I^2$. The next result asserts that fraudulent prescriptions of service is a persistent feature of competitive equilibrium in the credence good market. Formally,

Theorem 2: There exists no fraud-free equilibrium in the market for credence quality services.

While there exists no fraud-free equilibrium, the level of fraud committed depends on the stage game. In particular, since the supports of the equilibrium strategies is contained in $\{\omega_i, ..., \omega_n\}$, the larger is ω , the less room there is for fraudulent service overprescription.

4.2 Short-queue advantage and the evolution of the queues

The sole element of asymmetry between the suppliers in our model is the lengths of their queues. If $Q^A \neq Q^B$ the supplier with a shorter queue enjoys a strategic advantage in the sense that, if the two suppliers prescribe the same service, the supplier with the shorter queue is more likely to attract and retain a new customer. More generally, the short-queue advantage is measured by the *difference in the expected change of the lengths of the queues induced by equilibrium strategies.* Formally, given a stage game $\Gamma(\omega_i, Q^A, Q^B)$, if $Q^A < Q^B$ then the measure of the short-queue advantage is:

$$\Psi\left(\omega_{i}, Q^{A}, Q^{B} \mid \hat{\sigma}, \hat{G}\right) :=$$

$$\Sigma_{q \in Supp\hat{g}(\omega_{i}, Q^{A}, Q^{B})} \alpha^{A} \left(q \mid \hat{\sigma}, \hat{G}(\omega_{i}, Q^{B}, Q^{A}) q\hat{g}\left(\omega_{i}, Q^{A}, Q^{B}\right)(q)\right)$$

$$-\Sigma_{q \in Supp\hat{g}(\omega_{i}, Q^{B}, Q^{A})} \alpha^{B} \left(q \mid \hat{\sigma}, \hat{G}\left(\omega_{i}, Q^{A}, Q^{B}\right)\right) q\hat{g}\left(\omega_{i}, Q^{B}, Q^{A}\right)(q)$$

In the stationary setting of our model, in which no new suppliers enter and no existing supplier exits the market, the competition results in normal expected profits. We assume that the probability distribution of the random waiting time for the arrival of the next customer is time independent and has full support. Since the lengths of the queue are finite, starting from the event that both suppliers are idle (that is, $Q^A = Q^B = 0$) the probability, p, of returning to the same position under the equilibrium strategies is positive. Since the equilibrium is Markovian, this event is encountered infinitely often. Thus, the probability of the event " $Q^A = Q^B = 0$ infinitely often" is: $\lim_{m\to\infty} p^m > 0$. Hence, p = 1. In other words, starting from any state of the queues, $(Q^A, Q^B) \in I^2$, with probability one the queues will attain the point $Q^A = Q^B = 0$ infinitely often. From this position, the two suppliers are equally likely to become the long queue supplier. Hence, no supplier is *expected* to enjoys the short-queue advantage persistently. In other words, the evolution of the queues under the equilibrium strategies requires that the anticipated lengths of the queues be *stochastically equal*, in the sense that the identity of the short queue supplier is expected to change over time in such a way that the joint distribution of the queues is symmetric around its mean. We summarize this in the following:

Proposition 2. Under the equilibrium strategies, successive stage games induce a joint distribution of the lengths of the queues that is stationary, symmetric and the two suppliers commit the same amount of fraud on average.

The discussion above implies that an increase in the length of the queue of the short-queue supplier reduces its short-queue advantage. Formally, if A is the short queue supplier then $d\Psi\left(\omega_i, Q^A, Q^B \mid \hat{\sigma}, \hat{G}^A, \hat{G}^B\right)/dQ^A < 0$. However, because $d\alpha^A\left(q \mid \omega_i, \hat{G}\left(Q^B, Q^A, \hat{\sigma}\right)\right)/dQ^A < 0$ and $d\alpha^B\left(q \mid \omega_i, \hat{G}\left(Q^A, Q^B, \hat{\sigma}, \right)\right)/dQ^A > 0$, the short-queue advantage does not yield clear cut conclusions concerning its effect on the suppliers' equilibrium strategies.

5 Discussion

Our analysis shows that not only it is impossible for competition to sustain fraudfree equilibrium in the markets for credence goods that have the features depicted in this model but that, in fact, fraud is a persistent and prevalent phenomenon. The model in this paper envisages two suppliers engaged in Bertrand competition. The analysis highlights the role of the evolution of the customer's beliefs in the wake of her visit to the first supplier and the optimal stopping rule that characterized her best response strategy. The analysis also depicts the manner according to which the suppliers formulate their best response strategies given the information they possess. These aspects of our model and analysis are not specific to the two suppliers case and would show up, in a more complex form, if the number of the suppliers increase. Hence, there seems to be no essential loss of generality in so far as the main insights are concerned and much is gained by the relative simplicity afforded by considering two suppliers.

The model also highlight the advantage of the short-queue supplier and the consequent evolution of the queues. It is worth noting that if the waiting time is not an issue, that is, there is no capacity constraint, and each customer can be served immediately, then the analysis changes considerably. In this instance, the customers' utilities depend only on the prescribed service, and their discount rates is no longer a factor (that is, the customers' types are their idiosyncratic search cost, θ). Suppose that $\theta \in (0, 1]$ then it is easy to verify that the suppliers strategies $q^j(\omega_i) = \omega_n$, for all ω_i and $j \in \{A, B\}$, is an equilibrium. In other words, knowing that the prescription is the same, no customer is inclined to search and, consequently, the suppliers have no incentive to try and undercut each other's prescription. Maximal fraud also characterize the cab service provided to tourists in an unfamiliar city since the "diagnosis" (that is, the route taken) is identical to the service provided, leaving the customer no opportunity for seeking a second diagnosis. The route taken is only restricted by a tourist's conception of the reasonable length of the ride.¹⁷

One may think of variations on the model presented here. For instance, there are situations in which to obtain a diagnosis one has to schedule an appointment (e.g., a plumber service or medical examination). In these instances, the waiting time is ahead of obtaining the diagnosis and the customer may obtain information about the waiting time at different suppliers prior to deciding which supplier to visit first. This would change the information structure and, consequently, the strategies and equilibrium of the model. The analysis of such variations is left for future research.

An important aspect of the credence good market, discussed in Darby and Karni (1973) but not touched upon in this work, is the possibility of developing a reputation for honest diagnosis and its effect on the commission of fraud. Including reputation in our model would require admitting repeated interactions in which the customers display loyalty (that is, they visit "their" supplier first) and the suppliers recognize their loyal clients. Under these conditions, the suppliers may establish what Darby and Karni dubbed client relationship. The loss of future business of, and being bad-mouthed by, a dissatisfied customer would increase the cost to the suppliers of "losing" customers, which should serve as a deterrence and, consequently, mitigate the problem of fraud. This extension of the present work requires further study.

¹⁷See also, Stahl (1996) for a discussion of a related issue.

6 Proofs

6.1 Proof of Lemma 2

For $j \in \{A, B\}$, the customer's strategy affects V_k^j through the probability α_j in (7). Since V_k^j is continuous in α_j and α_j is continuous in σ_k , V_k^j is continuous in σ_k . To show that V_k^j is continuous in $G_k(\omega, Q^{-j}, Q^j)$, it suffices to show that

$$\int_{0}^{\infty} \left[v_{k}^{j} \left(Q^{j}, Q^{-j}, \omega_{i}, q \right) + e^{-rt'} \left[\sum_{\omega \in \Omega} V_{k}^{j} \left(Q^{j}(t'), Q^{-j}(t'), \omega_{j} \right) \mu(\omega) \right] dF(t')$$
(10)

is continuous in $G_k(\omega, Q^{-j}, Q^j)$. By equation (9), the expression in (10) depends on $G_k(\omega, Q^{-j}, Q^j)$ through $\sum_{q \in \Omega_{\omega_i}} V_k^j(\omega_i, Q^j, Q^{-j} + q) g_k(\omega, Q^{-j}, Q^j)(q)$. Since the last expression is linear in the probabilities $(g_k(\omega, Q^{-j}, Q^j)(q))_{q \in \Omega_{\omega_i}}$, it is continuous in $G_k(\omega, Q^{-j}, Q^j)$. That V_k^j is continuous in $G_k(\omega, Q^j, Q^{-j})$ follows from its linearity in the probabilities $(g_k(\omega, Q^j, Q^{-j})(q))_{q \in \Omega_{\omega_i}}$.

6.2 Proof of Theorem 1

Let $C_b^{I \times I}$ denote that set of bounded and continuous real-valued functions on the compact set $I \times I \times \Omega$. Thus, is compact by the product topology. Denote by G_k^j or g_k^j the strategies $G_k(\omega, Q^j, Q^{-j}), g_k(\omega, Q^j, Q^{-j}), j \in \{A, B\}$. Given $k \in N$, define a correspondence $T_k: (C_b^{I \times I})^2 \times \Delta(\Omega)^2 \times [0, 1] \Rightarrow (C_b^{I \times I})^2 \times \Delta(\Omega)^2 \times [0, 1]$ as follows:

$$T_k: \begin{pmatrix} V_k^A \\ V_k^B \\ G_k^A \\ G_k^B \\ \sigma_k \end{pmatrix} \rightrightarrows \begin{pmatrix} \bar{V}_k^A \\ \bar{V}_k^B \\ \bar{V}_k^B \\ \bar{G}_k^A \\ \bar{G}_k^B \\ \bar{\sigma}_k \end{pmatrix}$$

where the elements in the range set are defined as follows: Given $(V_k^j, G_k^{-j}, \sigma_k)$, $j \in \{A, B\}$,

$$\bar{V}_{k}^{j}\left(Q^{A}, Q^{B}, \omega_{i}\right) = \tag{11}$$

$$\max_{g_{k}^{j} \in \Delta(\Omega)} \sum_{q \in \Omega_{\omega_{i}}} \left[v_{k}^{j}\left(Q^{A}, Q^{B}, \omega_{i}, q\right) + \int_{0}^{\infty} e^{-rt'} \left[\sum_{\omega \in \Omega} V_{k}^{j}\left(Q^{A}(t'), Q^{B}(t'), \omega_{j}\right) \mu\left(\omega\right) \right] dF\left(t'\right) \right] g_{k}^{j}\left(q\right),$$

$$\bar{G}_{k}^{j} = \arg\max_{G_{k}^{j} \in \mathcal{G}_{k}} \sum_{q \in \Omega_{\omega_{i}}} \left[v_{k}^{j} \left(Q^{A}, Q^{B}, \omega_{i}, q \right) + \int_{0}^{\infty} e^{-rt'} \left[\sum_{\omega \in \Omega} V_{k}^{j} \left(Q^{A}(t'), Q^{B}(t'), \omega_{j} \right) \mu\left(\omega\right) \right] dF\left(t'\right) \right] g_{k}^{j}\left(q\right),$$

$$\tag{12}$$

where G_k^j is the CDF corresponding to g_k^j , and $\bar{\sigma}_k$ is the customer's best response given (G_k^A, G_k^B) . By Lemmata 1 and 2, for all $\omega, Q^A, Q^B \in \Omega \times I^2$, the function $\bar{V}_k^j : \Delta(\Omega)^2 \times \Sigma \to \mathbb{R}, \ j \in \{A, B\},$ in (11) and the customer's expected payoff, $\bar{U}: \Delta(\Omega)^2 \times \Sigma \to \mathbb{R}$ in (6) are continuous functions.

The sets of strategies of the suppliers and the customers are closed and bounded in \mathbb{R}^n . Hence, by the Heine-Borel theorem, they are compact. By definition and Berge maximum theorem, for $j \in \{A, B\}$, \bar{V}_k^j in (11) are continuous functions and the

correspondences \bar{G}_k^j in (12) are nonempty, compact and convex valued, and upper hemicontinuous. Moreover, by Proposition 1, the customer's strategy $\bar{\sigma}$ is singlevalued and is linear in the suppliers mixed strategies. Hence it is continuous in these strategies.

Since $\bar{V}_k^A, \bar{V}_k^B \in C_b^{I \times I}$ and $I \times I \times \Omega$ is compact, they attain their maximal and minimal values. Hence, the ranges of these functions are closed and bounded intervals in \mathbb{R} . Moreover, $\Delta(\Omega)$ and [0, 1] endowed with the Euclidean metric are compact metric spaces. Hence, the domain of the correspondence T_k is compact Housdorff space. By Kakutani's fixed point theorem, T_k has fixed point,

$$T_k: \begin{pmatrix} \hat{V}_k^A \\ \hat{V}_k^B \\ \hat{G}_k^A \\ \hat{G}_k^B \\ \hat{\sigma}_k \end{pmatrix} = \begin{pmatrix} \hat{V}_k^A \\ \hat{V}_k^B \\ \hat{V}_k^B \\ \hat{G}_k^A \\ \hat{G}_k^A \\ \hat{G}_k^B \\ \hat{\sigma}_k \end{pmatrix}.$$

By definition, a fixed point of the mapping T_k is a stationary Markov equilibrium point.

By compactness of the domain, every sequence, $(\hat{V}_k^A, \hat{V}_k^B, \hat{G}_k^A, \hat{G}_k^B, \hat{\sigma}_k)_{k \in N}$ of fixed points has convergent subsequence. Denote by $(\hat{V}^A, \hat{V}^B, \hat{G}^A, \hat{G}^B, \hat{\sigma})$ a subsequential limit point. We show next that $(\hat{G}^A, \hat{G}^B, \hat{\sigma})$ constitutes an equilibrium with respect to the value functions \hat{V}^A and \hat{V}^B and that (\hat{V}^A, \hat{V}^B) are the value functions corresponding to the strategies $(\hat{G}^A, \hat{G}^B, \hat{\sigma})$.

Let $\{k_n \mid n = 1, 2...\}$ be a convergent subsequence and consider supplier A. Given

$$\left(\hat{V}_{k_n}^A, \hat{V}_{k_n}^B, \hat{G}_{k_n}^A, \hat{G}_{k_n}^B, \hat{\sigma}_{k_n} \right), \text{ for all } G_{k_n}^A = \left(g_{k_n}^A \left(q \right) \right)_{q \in \Omega}, \text{ we have}$$

$$\Phi_{k_n}^A := \sum_{q \in \Omega_{\omega_i}} \left[\hat{v}_{k_n}^A \left(Q^A, Q^B, \omega_i, q \right) + \int_0^\infty e^{-rt'} \left[\sum_{\omega \in \Omega} \hat{V}_{k_n}^A \left(Q^A(t'), Q^B(t'), \omega_j \right) \mu\left(\omega\right) \right] dF\left(t'\right) \right] \hat{g}_{k_n}^A\left(q \right) \ge$$

$$\sum_{q \in \Omega_{\omega_i}} \left[\hat{v}_{k_n}^A \left(Q^A, Q^B, \omega_i, q \right) + \int_0^\infty e^{-rt'} \left[\sum_{\omega \in \Omega} \hat{V}_{k_n}^A \left(Q^A(t'), Q^B(t'), \omega_j \right) \mu\left(\omega\right) \right] dF\left(t'\right) \right] g^A\left(q\right) := \phi_{k_n}^A,$$

for all k_n , $n \in N$. Hence, $\lim_{n\to\infty} \Phi^A_{k_n} \geq \lim_{n\to\infty} \phi^A_{k_n}$. Let $\lim_{n\to\infty} \hat{G}^A_{k_n} = \hat{G}^A$, $\lim_{n\to\infty} \hat{G}^B_{k_n} = \hat{G}^B$, $\lim_{n\to\infty} \hat{\sigma}_{k_n} = \hat{\sigma}$ denote the limit strategies. Then,

$$\lim_{n \to \infty} \Phi_{k_n}^A = \sum_{q \in \Omega_{\omega_i}} \left[\hat{v}^A \left(Q^A, Q^B, \omega_i, q \right) + \int_0^\infty e^{-rt'} \left[\sum_{\omega \in \Omega} \hat{V}^A \left(Q^A(t'), Q^B(t'), \omega_j \right) \mu\left(\omega\right) \right] dF\left(t'\right) \right] \hat{g}^A\left(q\right),$$

where $\hat{V}^A\left(Q^A(t'), Q^B(t'), \omega_j\right) = \hat{V}^A\left(\hat{G}^A, \hat{G}^B, \hat{\sigma} \mid Q^A(t'), Q^B(t'), \omega\right)$. Note also that $\lim_{n\to\infty} \phi_{k_n}^A$ is the value function of player A of the strategy G^A when player B and the customer play the limit strategies \hat{G}^B and $\hat{\sigma}$, respectively, given the continuation function \hat{V}^A . Thus, $\lim_{n\to\infty} \Phi_{k_n}^A \ge \lim_{n\to\infty} \phi_{k_n}^A$ implies that \hat{G}^A is best response to \hat{G}^B and $\hat{\sigma}$, given the continuation function \hat{V}^A . Repeating the same argument for supplier B we conclude that \hat{G}^B is best response to \hat{G}^A and $\hat{\sigma}$, given the continuation function \hat{V}^B . That $\hat{\sigma}$ is best response to \hat{G}^A and \hat{G}^B is obvious.

Finally, since $\hat{V}^{j}\left(Q^{A}, Q^{B}, \omega_{j}\right) = \hat{V}^{j}\left(\hat{G}^{A}, \hat{G}^{B}, \hat{\sigma} \mid Q^{A}, Q^{B}, \omega\right), \ j \in \{A, B\}, \ \hat{V}^{A}$ and \hat{V}^{B} are the value functions corresponding to the strategies $\left(\hat{G}^{A}, \hat{G}^{B}, \hat{\sigma}\right)$. \Box

6.3 Proof of theorem 2

Fraud-free equilibrium in the credence-good market requires that, $\hat{G}(\omega, Q^j, Q^{-j}) = \delta_{\omega}$, for all $(\omega, Q^j, Q^{-j}) \in \Omega \times I^2$ and $j \in \{A, B\}$. To prove that there is no fraud-free equilibrium we need to show that, for some stage game $\Gamma(\omega, Q^A, Q^B)$, $\hat{G}(\omega, Q^j, Q^{-j}) = \delta_{\omega}$ is not a best response to $\hat{G}(\omega, Q^{-j}, Q^j) = \delta_{\omega}$, for some $j \in \{A, B\}$.

Suppose that there is fraud-free equilibrium (that is, $\hat{G}(\omega, Q^j, Q^{-j}) = \delta_{\omega}$, for all Q^j and Q^{-j} , $j \in \{A, B\}$) and consider the case $Q^A = 0 < Q^B$. In fraud-free equilibrium the customers believe that both suppliers prescribe the necessary service truthfully. Hence, the only reason to obtain a second prescription is the expectations that the second supplier has a sufficiently shorter queue that would justify bearing the cost of obtaining a second prescription. Thus, the probability of a new customer accepting the prescription ω from the long-queue supplier is as follows.

If the long-queue supplier (that is, supplier B) is the customer's first call then the probability of acceptance is:

$$p_1\left(Q^B\right) := \xi\{(\theta, \beta) \in T \mid e^{-\beta Q^B} > \theta E\left[e^{-\beta Q} \mid Q^B\right]\},\$$

where $E\left[e^{-\beta Q} \mid Q^B\right] = \int_0^\infty e^{-\beta Q} \upsilon\left(Q \mid Q^B\right) dQ$ and $\upsilon\left(Q \mid Q^B\right)$ is the distribution of supplier *A*'s queue conditional on Q^B .

If the customer visits the short-queue supplier (that is, supplier A) first, the probability that he eventually accepts the prescription ω of the long-queue supplier requires that his type (θ, β) satisfies $e^{-\beta Q^A} < \theta E \left[e^{-\beta Q} \mid Q^A \right]$ and $w(q_A) e^{-\beta Q^A} <$ $\theta w(\omega) e^{-\beta Q^B}$. The probability of this event is

$$p_2\left(\omega, Q^A, Q^B, q_A\right) := \xi\{(\theta, \beta) \in T \mid e^{-\beta Q^A} < \theta E\left[e^{-\beta Q} \mid Q^A\right] \text{ and } w\left(q_A\right)e^{-\beta Q^A} < \theta w\left(\omega\right)e^{-\beta Q^B}\}.$$

Define $p_B(\omega, Q^A, Q^B, q_A) = p_1(Q^B) + p_2(\omega, Q^A, Q^B, q_A)$. Then the short-queue supplier's expected profit is given by:

$$\max_{q_A \ge \omega} \left[\left(1 - p_B\left(\omega, Q^A, Q^B, q_A\right) \right) V\left(Q^A + q_A, Q^B \right) + p_B\left(\omega, Q^A, Q^B, q_A\right) V\left(Q^A, Q^B + \omega \right) \right].$$

But $Q^A = 0$ implies that $e^{-\beta Q^A} > \theta e^{-\beta Q^B}$ and $e^{-\beta Q^A} > \theta E \left[e^{-\beta Q} \mid 0 \right]$, for all $\beta > 0$. Hence, $p_2 \left(\omega_i, Q^A, Q^B, \omega_{i+1} \right) = 0$ and, since $p_1 \left(Q^B \right)$ is independent of q_A , $p_B \left(\omega_i, Q^A, Q^B, \omega_{i+1} \right) = p_B \left(\omega_i, Q^A, Q^B, \omega_i \right)$. Since $V \left(Q^A + \omega_{i+1}, Q^B \right) - V \left(Q^A + \omega_i, Q^B \right) > 0$, $\hat{G} \left(\omega_i, 0, Q^B \right) = \delta_{\omega_i}$ is not best response to δ_{ω_i} .

References

- Akerlof, George, A. (1970) "The Market for "Lemons": Quality Uncertainty and the Market Mechanism," *The Quarterly Journal of Economics* 84, 488-500.
- [2] Aliprantice, Charalambos, D. and Border, Kim C. Infinite Dimensional Analysis. (3rd edition) 2006 Springer, Berlin.
- [3] Balafoutas, Loukas, Beck Adrian, Kerschbamer Rudolf and Sutter Matthias (2013) "What Drives Taxi Drivers? A Field Experiment on Fraud in a Market for Credence Goods," *The Review of Economic Studies*, 80, 876–891.
- [4] Beck, Adrian, Kerschbamer, Rudolf, Qiu Jianying, and Sutter, Matthias (2014) "Car Mechanics in the Lab: Investigating the Behavior of Real Experts on Experimental Markets for Credence Goods," Working Papers in Economics and Statistics, 2014-02, University of Innsbruck.
- [5] Currie, Janet. Lin, Wanchuan, and Zhang, Wei. (2011) "Patient Knowledge and Antibiotic Abuse: Evidence From an Audit Study in China," *Journal of Health Economics*, 30, 933-949.
- [6] Darby, Michale and Karni, Edi (1973) "Free Competition and the Optimal Amount of Fraud," Journal of Law and Economics XVI: 67-88.
- [7] Dranove, D. (1988) "Demand Inducement and the Physician/Patient Relationship," *Economic. Inquiry*, 26, 281-298.
- [8] Dulleck, Uwe and Kerschbamer Rudolf (2006) "On Doctors, Mechanics, and

Computer Specialists: The Economics of Credence Goods," *Journal of Economic Literature* 44: 5-42.

- [9] Domenighetti G, Casabianca A, Gutzwiller F, Martinoli S. (1993) "Revisiting the Most Informed Consumer of Surgical Services. The Physician-Patient," Internationa Journal of Technology Assessment Health Care, 9(4). 505-13.
- [10] Emons, Winand (1997) "Credence Goods and Fraudulent Experts," The RAND Journal of Economics, 28: 107-119.
- [11] Fong, Yuk-fai, and Liu, Ting (2016) "Liability and Reputation in Credence Goods Markets," *Economics Letters*, 166, 35-39.
- [12] Fong, Yuk-fai, Hu, Xiaoxiao, Liu, Ting and Meng, Xiaoxuan (2017) "Using Customer Service to Build Client Trust," *Journal of Industrial Economics* (forthcoming)
- [13] Heinzel, Joachim (2019) "Credence Good Market with Heterogeneous Expert," Universitat Paderborn, Center for International Economics, Working Paper No. 2019-01.
- [14] Hu, Xiaoxiao and Lin, Jialiang (2018) "Verifiability and Fraud in a Dynamic Credence Goods Market," unpublished manuscript.
- [15] Iizuka, Toshiaki (2007) "Experts' Agency Problems: Evidence from the Prescription Drug Market in Japan," The RAND Journal of Economics 38, 844-862.
- [16] Mcguire, Thomas G. (2000) "Physician Agency" Handbook of Health Economics Culver Anthony J. and Joseph Newhouse P. (eds.) Volume 1: 461-536.

- [17] Stahl, Dale O. (1996) "Oligopolistic Pricing with Heterrogeneous Consumer Search," International Journal of Industrial Organization, 14: 243-268.
- [18] Wolinsky, Asher (1993) "Competition in A Market for Informed Experts' Services," The Rand Journal of Economics, 24: 380-398
- [19] Wolinsky, Asher (1995) "Competition in Markets for Credence Goods," Journal of Institutional and Theoretical Economics 151: 117-131.